

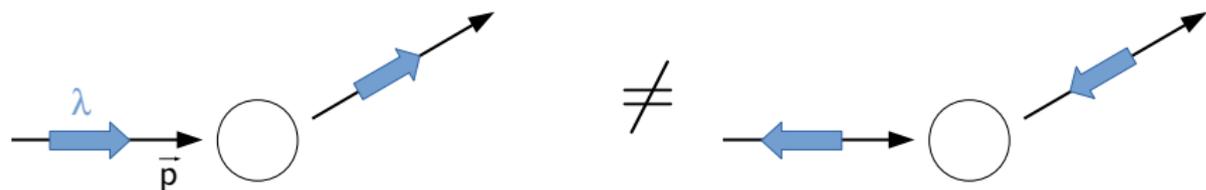
Weak Neutral Current Studies with Positrons

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Parity Violation in Electron Scattering



- Weak force couplings provide unique mode to study nature
- Charged current (e.g. β decay) maximally violating, but neutral current mixed by weak mixing angle $\sin^2 \theta_W$
- Arises in low Q^2 e^- scattering as interference between γ and Z
- Basic object of study is PV asymmetry

$$\frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L} = A_{PV} = \frac{\left| \begin{array}{c} \gamma^* \\ Z^0 \end{array} \right|^* \left| \begin{array}{c} \gamma^* \\ Z^0 \end{array} \right|}{\left| \begin{array}{c} \gamma^* \end{array} \right|^2} \sim \frac{G_F Q^2}{\sqrt{2}\pi\alpha} \times \dots = 10^{-6} \sim 10^{-3}$$

Neutral Current Structure and Positrons

- Standard e^- parity violating asymmetry typically has two terms

$$A = \frac{R - L}{R + L} \sim \frac{G_F Q^2}{\sqrt{2}\pi\alpha} \left[D_f(\theta) g_A^e g_V^{\text{target}} + D_b(\theta) g_V^e g_A^{\text{target}} \right]$$

$$g_A = T_3 \quad g_V = T_3 - 2Q \sin^2 \theta_W$$

$$T_3 \sim \begin{pmatrix} \nu_l \\ l^- \end{pmatrix}_L, \begin{pmatrix} u \\ d \end{pmatrix}_L, \dots$$

- Second term is typically harder to get to kinematically
 - Requires kinematic separation
 - g_V^e is ~ 0.1 , g_V^q larger
- Axial terms under C effectively $g_A \rightarrow -g_A$

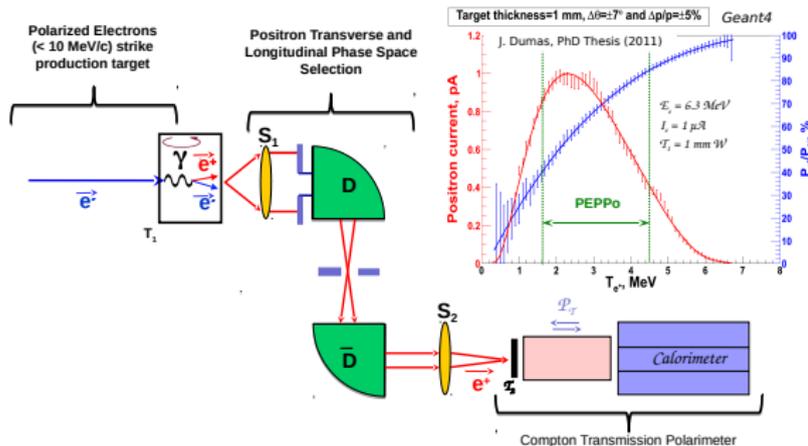
Neutral Current Structure and Positrons (II)

- $e^+(R/L) - e^-(L/R)$ asymmetry offers unique interesting combination

$$\Delta = (\pm g_V^e + g_A^e) G_A^{\text{target}}(x, Q^2) \times \dots$$

- axial-axial coupling unique and not suppressed by $1 - 4 \sin^2 \theta_W$!
- Don't actually need spin for separation - relative intensity control must be much better than asymmetry
- Axial term of targets is has interesting physics opportunities
 - DIS - C_{3q} couplings
 - $q - \bar{q}$ pdfs
 - ep - Direct access to axial form factor
- Other opportunities
 - Sign flip in EM higher order effects
 - s-channel studies

PEPPo Principle of Operation



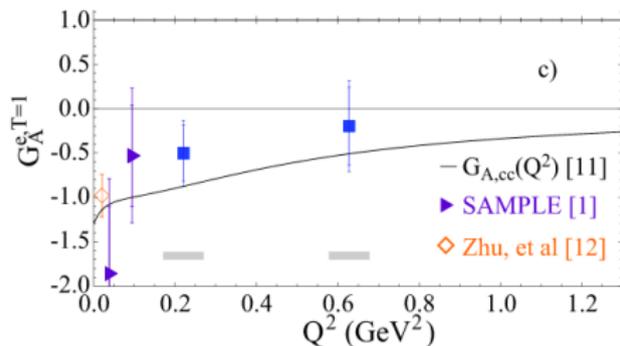
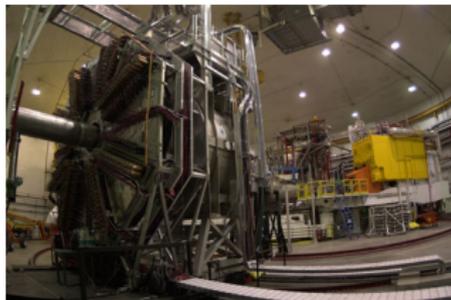
PEPPo measured the longitudinal polarization transfer from 8.25 MeV/c e^- to e^+ in the 3.07-6.25 MeV/c momentum range.



L. S. Cardman (JPos17)



- 100 nA 60% polarization
- 1 μA unpolarized



$$A = \left[\frac{-G_F Q^2}{4\pi\alpha\sqrt{2}} \right] \left[\frac{\epsilon G_E^\gamma G_E^Z + \tau G_M^\gamma G_M^Z + 2g_V^e \epsilon' G_M^\gamma G_A^Z}{\epsilon (G_E^\gamma)^2 + \tau (G_M^\gamma)^2} \right]$$

$$\epsilon = \left[1 + 2(1 + \tau) \tan^2 \frac{\theta}{2} \right]^{-1}; \quad \epsilon' = \sqrt{\tau(1 + \tau)(1 - \epsilon^2)}; \quad \tau = Q^2/4M^2$$

$$G_E^{pZ} = (1 - 4 \sin^2 \theta_W) G_E^{p\gamma} - G_E^{n\gamma} - G_E^{s\gamma}$$

- G0 covered Q^2 0.1-1 GeV^2 at various
- Two backwards angle runs on LH₂ and QE LD₂
- Extracted G_A with considerable uncertainty
Axial $\sim 20\%$ contribution to proton asymmetry

- Axial form factor measured in β decay only **isovector** component with $n \rightarrow p$ by SU(3)
- Related to spin structure and DIS

$$\Gamma_1^p = \int_0^1 \sum e_i \Delta q_i(x) dx \sim \frac{1}{12} g_A^{(3)} + \frac{1}{36} g_A^{(8)} + \frac{1}{9} g_A^{(0)} + \dots$$

- Proton neutral current G_A includes isoscalar components (i.e. strange quarks and also radiative components)

$$G_A^p(Q^2 = 0) = g_A^{(3)} \left(1 + R_A^{T=1}\right) + \frac{3F - D}{2} R_A^{T=0} + \Delta s \left(1 + R_A^{(0)}\right)$$

$$\Delta s = g_A^{(8)} - g_A^{(0)}$$

Radiative Corrections

- Radiative corrections to Axial FF not well known, difficult to calculate (Zhu et al, PRD 62 (2000) 033008)

$$\frac{R_A^{T=1}}{-0.258(0.34)} \quad \frac{R_A^{T=0}}{-0.239(0.2)} \quad \frac{R_A^0}{-0.551}$$

- Typically only small suppressed component in forward experiments
- In positron measurement targeting axial FF, on the order 10%

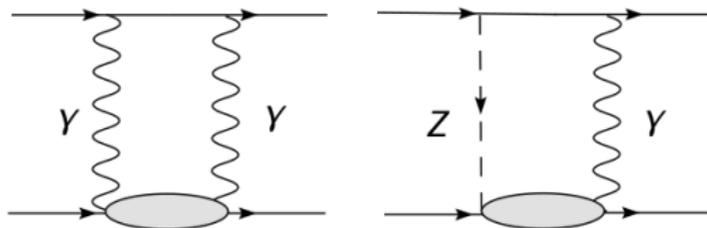
$$A^{e^+e^-} = \frac{G_F Q^2}{2\pi\alpha\sqrt{2}} g_A^e \frac{G_A^Z G_M^\gamma}{\epsilon (G_E^\gamma)^2 + \tau (G_M^\gamma)^2}$$

- **Totally overwhelmed by $\gamma\gamma$ terms**
- 6 μA , trying to get 10% measurement of G_A^Z , similar G0 kinematic run time ignoring 2γ ...
- A_{PV} radiative corrections (e.g. $\gamma - Z$ box diagrams) V and A corrections have positron sign flip in each single measurement not enough to constrain (Afanasev, Carlson PRL 94 212301 (2005))

Radiative Corrections

- Exception for spinless targets \rightarrow no axial current
- Sensitive to box of extra photon

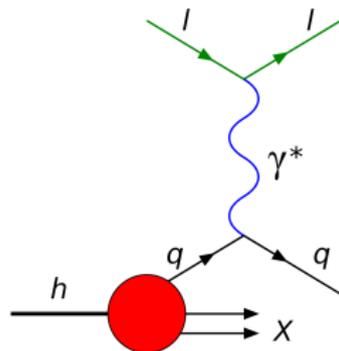
$$A_{\text{extra photon}} = A_{\text{PV}}^{e^+} + A_{\text{PV}}^{e^-}$$



Afanasev, Carlson PRL 94 212301 (2005)

PVDIS - Deep Inelastic Scattering

- PVDIS gives access to underlying partonic structure
- Rate at high $Q^2 \rightarrow$ relatively larger statistics and asymmetry
- $A_e V_q$ (C_{1q}) and $V_e A_q$ (C_{2q}) effective couplings
- Excellent combination to test new physics and QCD nucleon/nuclear structure!



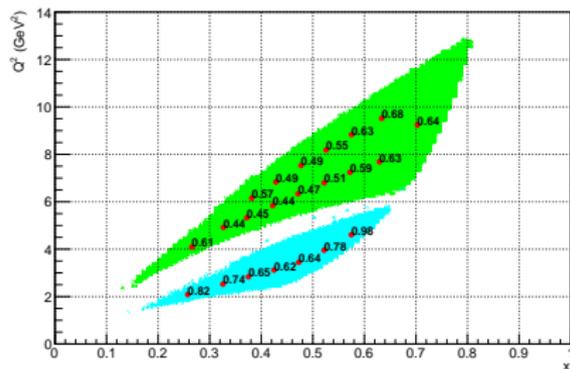
$$A_{PV} \approx -\frac{G_F Q^2}{4\sqrt{2}\pi\alpha} \left[a_1(x) + \frac{1 - (1-y)^2}{1 + (1-y)^2} a_3(x) \right], y = 1 - \frac{E'}{E}$$

$$a_1(x) = 2 \frac{\sum C_{1q} e_q (q + \bar{q})}{\sum e_q^2 (q + \bar{q})}, a_3(x) = 2 \frac{\sum C_{2q} e_q (q - \bar{q})}{\sum e_q^2 (q + \bar{q})}$$

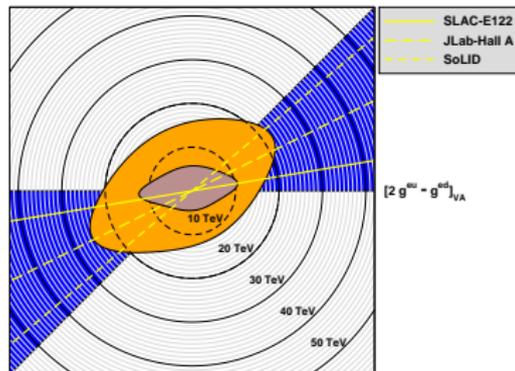
$$\begin{aligned} C_{1u} &= -\frac{1}{2} + \frac{4}{3} \sin^2 \theta_W = -0.19 & C_{2u} &= -\frac{1}{2} + 2 \sin^2 \theta_W = -0.03 \\ C_{1d} &= \frac{1}{2} - \frac{4}{3} \sin^2 \theta_W = 0.34 & C_{2d} &= \frac{1}{2} - 2 \sin^2 \theta_W = 0.03 \end{aligned}$$

SoLID - PVDIS SM and Nucleon Properties

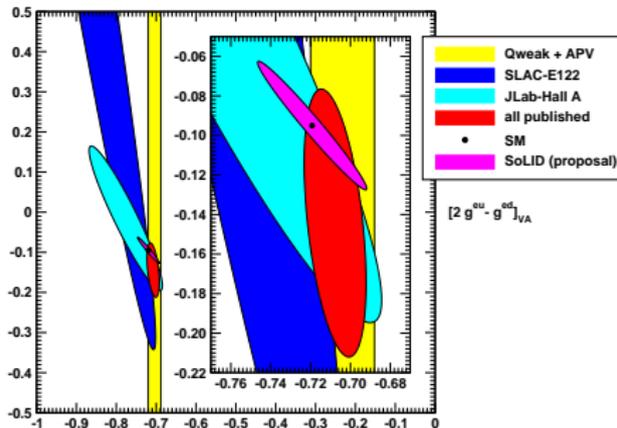
PVDIS Asymmetry Uncertainty (%)



$[2 g^{\text{uu}} - g^{\text{dd}}]_{\text{AV}}$



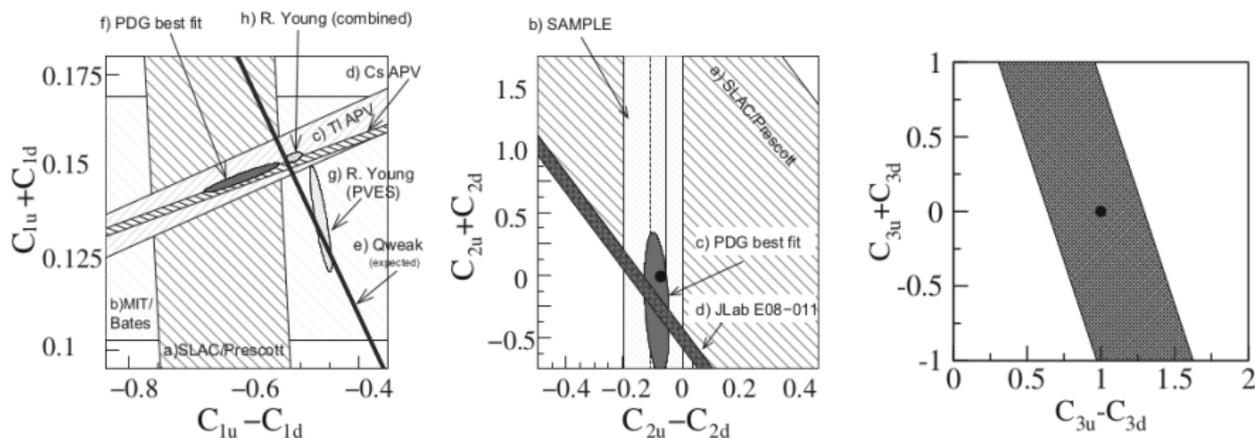
$[2 g^{\text{uu}} - g^{\text{dd}}]_{\text{AV}}$



- $60 \mu\text{A}$ on 40 cm LH_2 or LD_2 target
- Errors for 120 days 11 GeV LD_2 give sub 1% in many bins
- Constraints on $\Lambda \sim 10\text{-}20 \text{ TeV}$

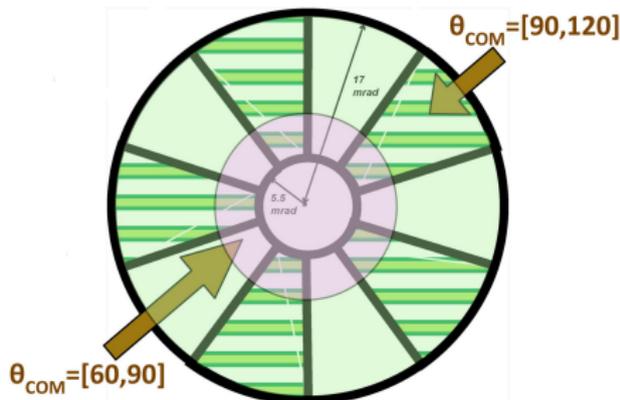
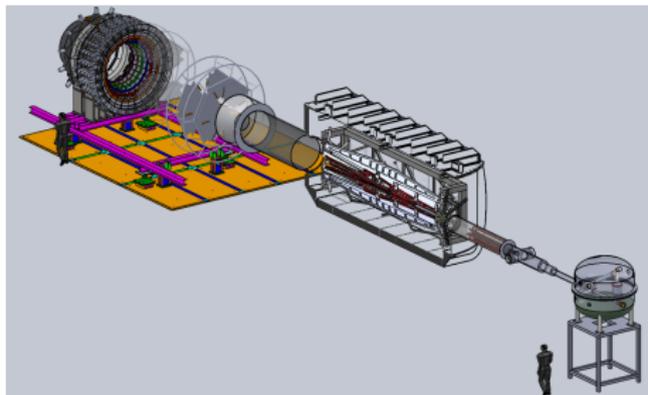
Axial-Axial in DIS has effective couplings $C_{3q} = \pm \frac{1}{2}$

$$A^{e^+(R/L)-e^-(L/R)} = \frac{G_F Q^2}{4\sqrt{2}\alpha\pi} \frac{1 - (1-y)^2}{1 + (1-y)^2} \frac{\sum (C_{2q} \pm C_{3q}) e_q(q - \bar{q})}{\sum e_q^2(q + \bar{q})}$$



- Only measured once at CERN with μ^+ and μ^- on C to $\sim 25\%$ level
- To get few % measurement of $2C_{3u} - C_{3d}$ on LD₂, 30 days 6 μA with SoLID
- Asymmetries on the order of 100 s ppm - beam quality systematics are less stringent

MOLLER → BHABHA?



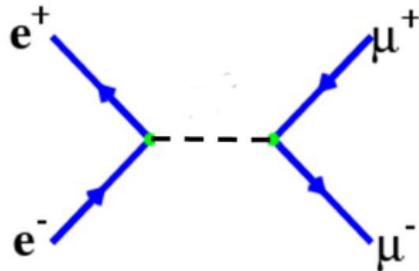
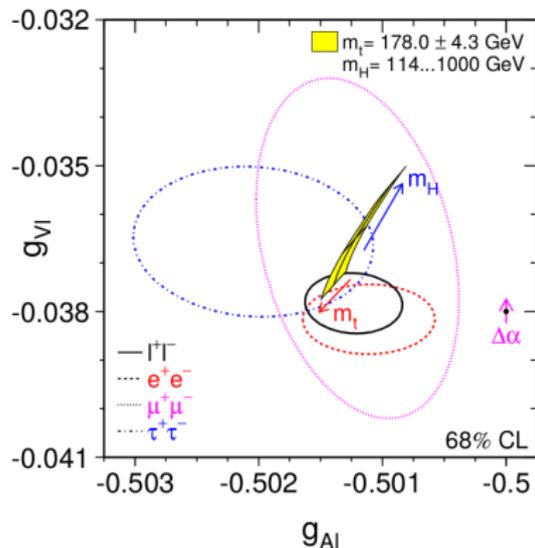
- $\sin^2 \theta_W$ to new world leading precision
- 11 GeV beam on 150 cm LH₂ target with accepted $\theta = 6 - 17$ mrad
- $A_{PV} = 35$ ppb to 2.1%

$$A_{ee} = m_e E \frac{G_F}{\sqrt{2}\pi\alpha} \frac{4 \sin^2 \theta_{CoM}}{(3 + \cos^2 \theta_{CoM})^2} (1 - 4 \sin^2 \theta_W)$$

- Symmetric in electrons - already have access to product $g_A^e g_V^e$ so probably not a lot interesting

$$e^+e^- \rightarrow f\bar{f}?$$

Other couplings to fermions not as well measured!

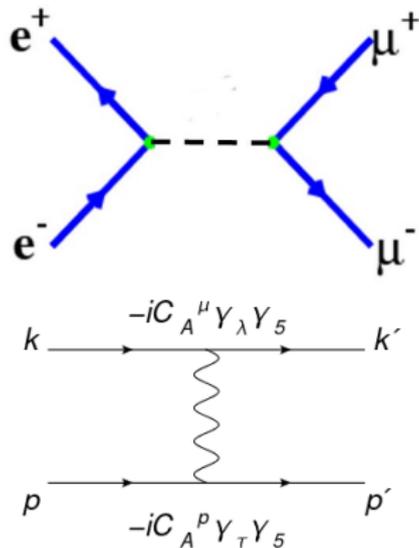
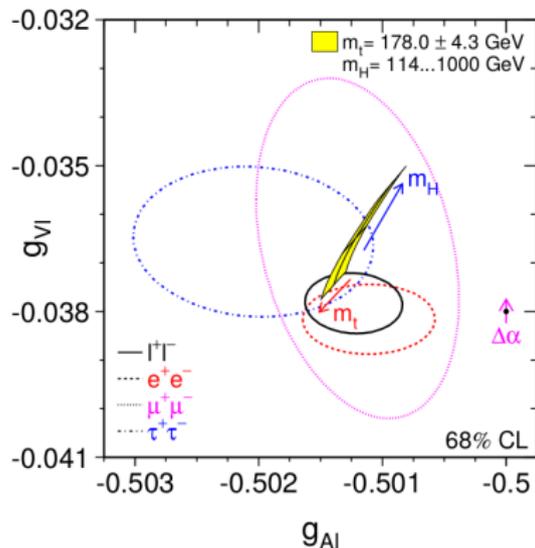


$$A_{\text{LRFB}} \sim \frac{g_V/g_A}{1 + (g_V/g_A)^2}$$

- Interesting for proton radius puzzle? (maybe in loops?)
- Need $4m_\mu^2 < s = 2m_e E \sim 43 \text{ GeV}$ e^+ to do this on fixed target...
- Statistics for colliders off Z resonance too challenging

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