

PR12-25-010, JLab PAC 53

Double Deeply Virtual Compton Scattering with SoLID μ spectrometer

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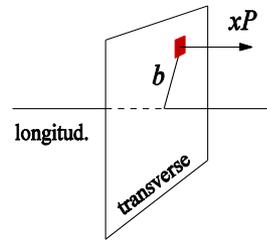
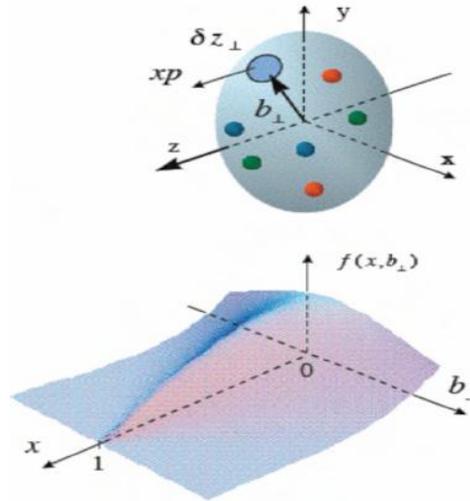
July 21, 2025

Outline

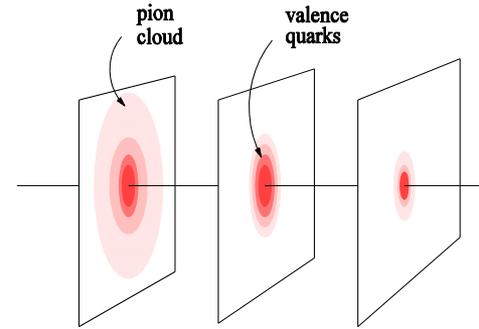
- Generalized Parton Distribution
- Double Deeply Virtual Compton Scattering
- SoLID μ setup
- Muon detector
- Simulation study
- Physics projection
- Beam time request
- Summary

Generalized Parton Distribution (GPD)

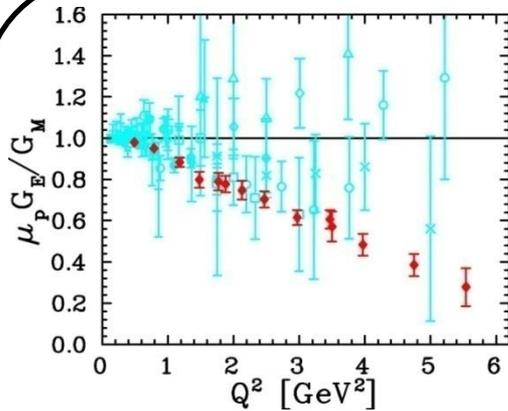
A unified description of partons (quarks and gluons) in the momentum and impact parameter space



(a)

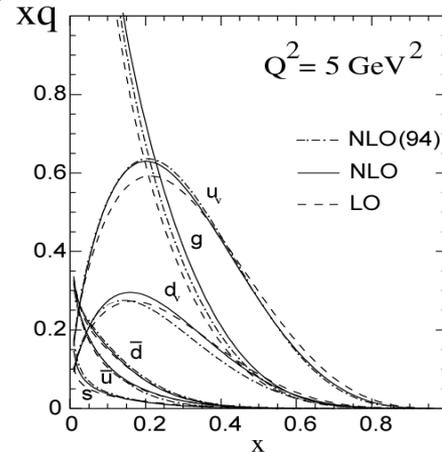
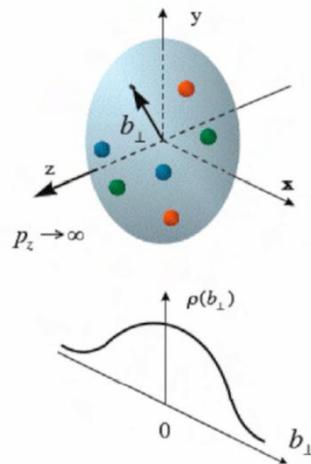


(b) $x < 0.1$ $x \sim 0.3$ $x \sim 0.8$



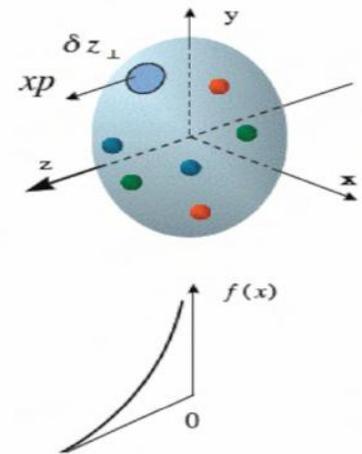
Elastic form factors

Transverse spatial distributions



Parton Distribution Functions

Longitudinal momentum distributions



Nucleon Structure and GPD

GPDs encode **correlations between partons** and contain information about **internal dynamics of hadrons** like **angular momentum** or **distribution of the forces** experienced by quarks and gluons

imaging

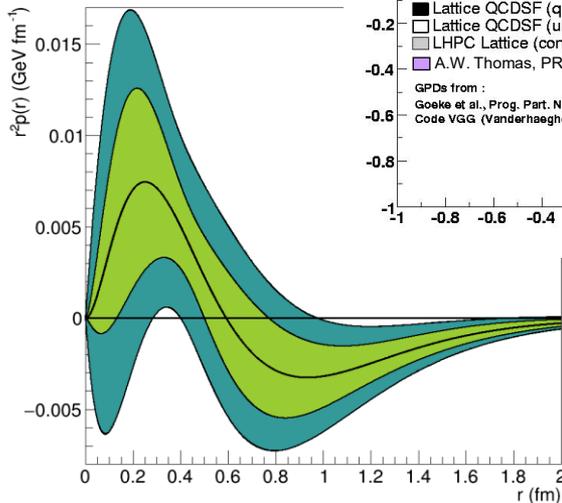
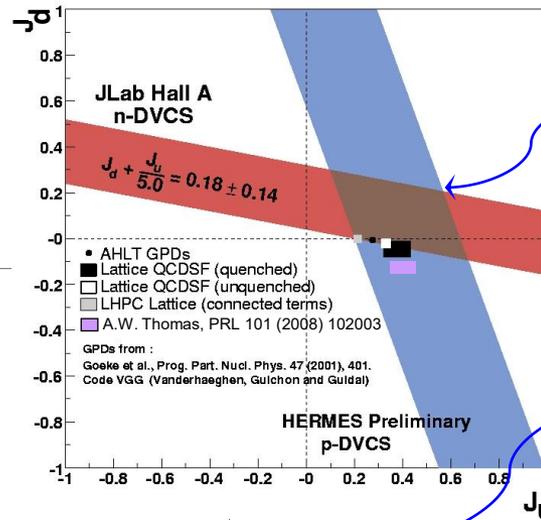
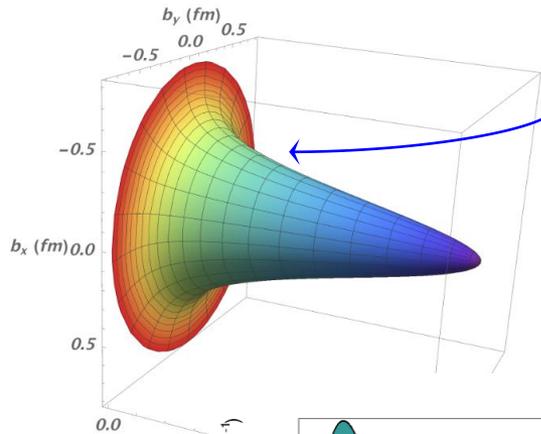
$$\rho_H^q(x, \mathbf{b}_\perp) = \int \frac{d^2 \Delta_\perp}{(2\pi)^2} e^{i\mathbf{b}_\perp \cdot \Delta_\perp} [H^q(x, 0, -\Delta_\perp^2) + H^q(-x, 0, -\Delta_\perp^2)]$$

spin

$$\lim_{t \rightarrow 0} \int_{-1}^1 x [H^q(x, \xi, t) + E^q(x, \xi, t)] dx = J^q$$

gravitational form factor

$$\int_{-1}^1 x \sum_q H^q(x, \xi, t) dx = M_2(t) + \frac{4}{5} \xi^2 d_1(t)$$



The **experimental knowledge** of the **ξ -dependence** of GPDs at fixed longitudinal momentum fraction is a **crucial step** for unraveling the 3D structure and internal dynamics of the **nucleon**

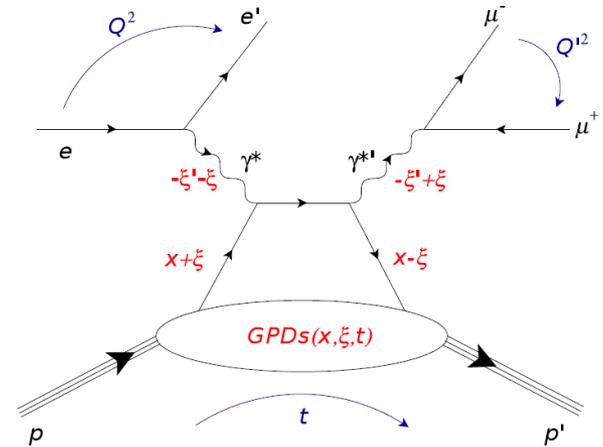
General Compton Process accessing GPD

$$\gamma^*(q) + p(p) \rightarrow \gamma^*(q') + p(p')$$

$$Q^2 = -q^2, \quad Q'^2 = q'^2, \quad s = (p + q)^2, \quad t = \Delta^2,$$

DVCS	$(\gamma^* \rightarrow \gamma, Q'^2=0, \xi' = \xi)$
Timelike CS	$(\gamma \rightarrow \gamma^*, Q^2=0, \xi' = -\xi)$
Double DVCS	$(\gamma^* \rightarrow \gamma^*, Q^2 Q'^2 \xi' \xi \text{ vary})$

Because of the virtuality of the initial and final photon, **DDVCS** allows direct access to GPDs at $|x| < \xi$, crucial for modeling and investigation of **nuclear imaging, spin, and internal dynamics**



Compton Form Factor (CFF)

$$\mathcal{F}(\xi', \xi, t) = \mathcal{P} \int_{-1}^1 F_+(x, \xi, t) \left[\frac{1}{x - \xi'} \pm \frac{1}{x + \xi'} \right] dx - i\pi F_+(\xi', \xi, t)$$

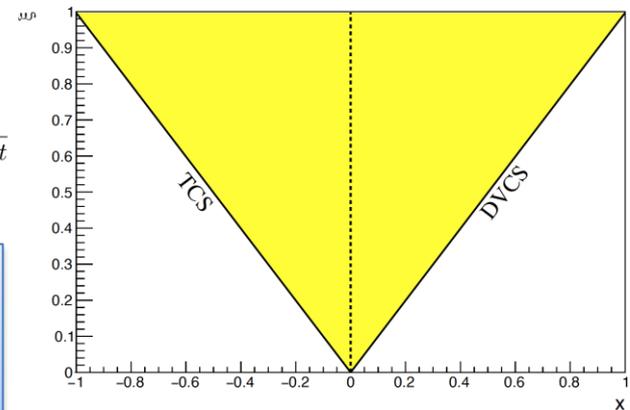
GPD combination

$$F_+(x, \xi, t) = \sum_q \left(\frac{e_q}{e} \right)^2 [F^q(x, \xi, t) \mp F^q(-x, \xi, t)]$$

Generalized

Bjorken variable $\xi' = \frac{Q^2 - Q'^2 + t/2}{2Q^2/x_B - Q^2 - Q'^2 + t}$ Skewness $\xi = \frac{Q^2 + Q'^2}{2Q^2/x_B - Q^2 - Q'^2 + t}$

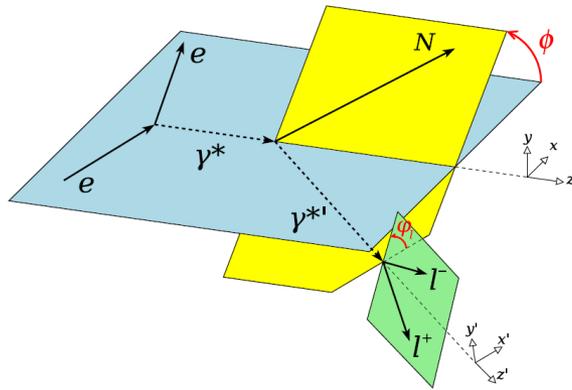
Following the sign change of ξ' around $Q'^2=Q^2$, the imaginary part of \mathcal{H} and \mathcal{E} **change sign**, providing a testing ground of **GPD universality**.



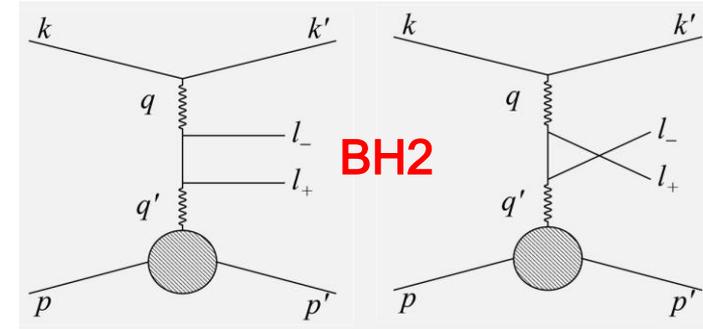
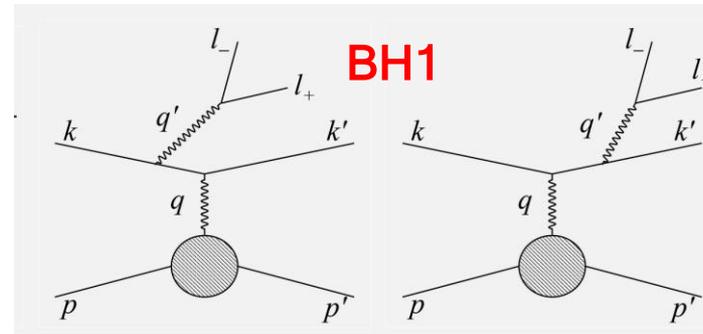
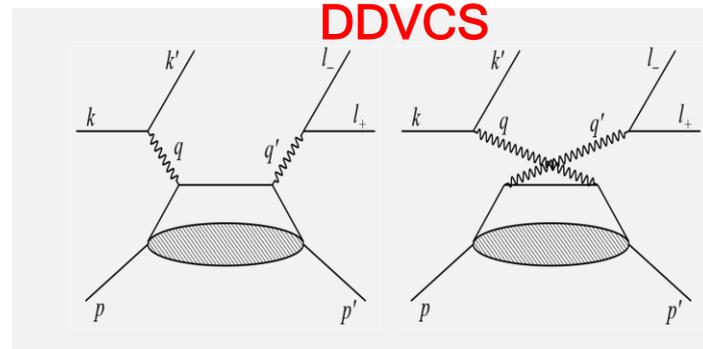
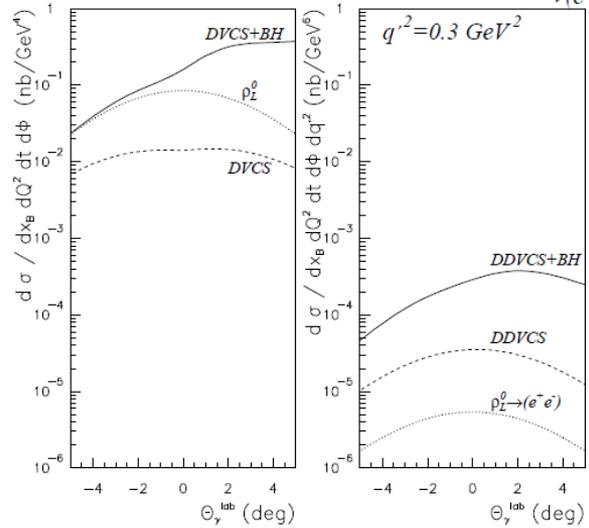
Elementary Cross Section

DDVCS cross section is about $\sim 1/100$ of **DVCS**, involves two Bethe-Heitler (BH) processes

$$d^7\sigma_P^e = d^7\sigma_{BH_1} + d^7\sigma_{BH_2} + d^7\sigma_{DDVCS} + P d^7\tilde{\sigma}_{DDVCS} + d^7\sigma_{INT_2} + P d^7\tilde{\sigma}_{INT_2} - e [d^7\sigma_{BH_{12}} + d^7\sigma_{INT_1} + P d^7\tilde{\sigma}_{INT_1}]$$



$E_e = 6 \text{ GeV}, Q^2 = 2.5 \text{ GeV}^2, x_B = 0.3, \Phi = 0 \text{ deg.}$
 $\bar{e} + p \rightarrow \bar{e} + p + \gamma, \rho_L^0 \quad \bar{e} + p \rightarrow \bar{e} + p + (\gamma, \rho_L^0)$
 $\rightarrow (\bar{e} e^+)$



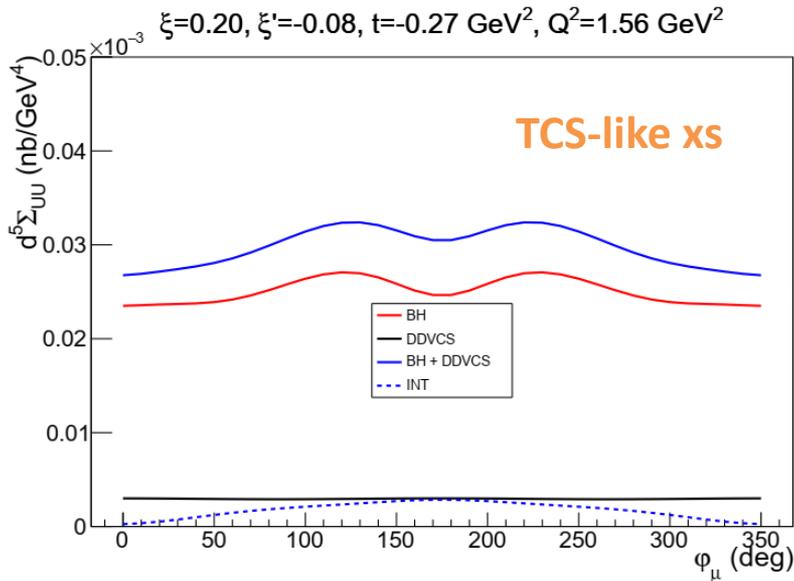
Integrated Cross Section

5-fold TCS-like observables obtained from the **integration** over the **polar angle** of **muon** and the **azimuthal angle** of **initial virtual photon**, also **minimizing** the contribution of the **BH₂** process

$$\theta_0 = \pi/4$$

$$d^5\Sigma^\lambda(\varphi_\mu) \equiv \frac{d^5\sigma^\lambda(\varphi_\mu)}{dx_B dy dt dQ'^2 d\varphi_\mu} = \int_0^{2\pi} d\phi \int_{\pi/2-\theta_0}^{\pi/2+\theta_0} d\theta_\mu \sin(\theta_\mu) \frac{d^7\sigma^\lambda(\phi, \theta_\mu, \phi_\mu)}{dx_B dy dt d\phi dQ'^2 d\Omega_\mu}$$

$$d^5\Sigma^\lambda = d^5\Sigma_{BH_1} + d^5\Sigma_{BH_2} + d^5\Sigma_{BH_{12}} + d^5\Sigma_{DDVCS} + d^5\Sigma_{\mathcal{I}_1} + d^5\Sigma_{\mathcal{I}_2} + \lambda d^5\tilde{\Sigma}_{\mathcal{I}_2} = d^5\Sigma_{UU} + \lambda d^5\Sigma_{LU}$$



- Our study focuses on using **TCS-like observables** for projection to allow access to both terms above
- DVCS-like observables obtained by integrating over muon phi angle may also be considered as crosscheck

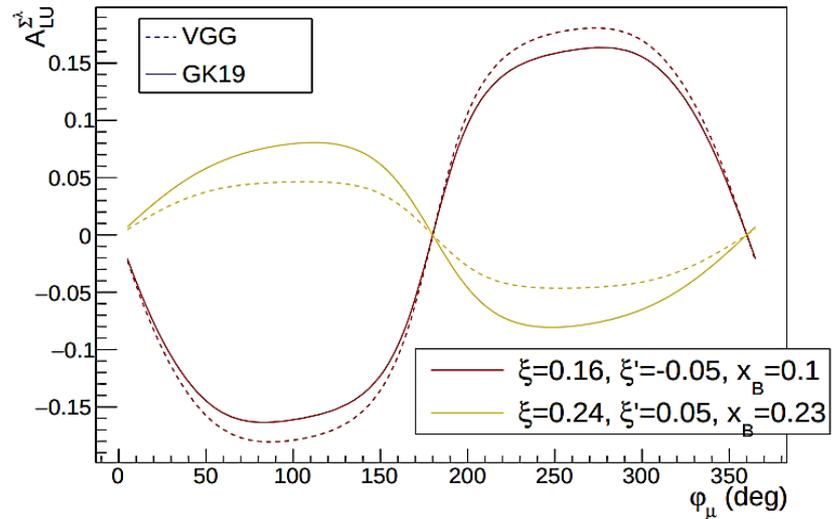
Beam Spin Asymmetry

$$A_{LU}^{\Sigma\lambda}(\varphi_\mu) = \lambda \frac{d^5\Sigma^+ - d^5\Sigma^-}{d^5\Sigma^+ + d^5\Sigma^-} = \frac{\lambda d^5\tilde{\Sigma}_{\mathcal{I}_2}}{d^5\Sigma_{BH_1} + d^5\Sigma_{BH_2} + d^5\Sigma_{BH_{12}} + d^5\Sigma_{DDVCS} + d^5\Sigma_{\mathcal{I}_1} + d^5\Sigma_{\mathcal{I}_2}}$$

$$\propto \Im \left\{ F_1 \mathcal{H} + \xi' (F_1 + F_2) \tilde{\mathcal{H}} - \frac{t}{4M_N^2} F_2 \mathcal{E} \right\}$$

- Access to the imaginary part of CFFs
- **BSA** changes sign when transitioning from **DVCS-like region** ($\xi' > 0, Q^2 > Q'^2$) to **TCS-like region** ($\xi' < 0, Q^2 < Q'^2$)
- **DDVCS BSAs** are dominated by the CFF \mathcal{H} , thus providing a measurement of the \mathcal{H} GPD at $\xi' \neq \pm \xi$ with similar quality to DVCS

BSA in two regions



Muon Charge Asymmetry

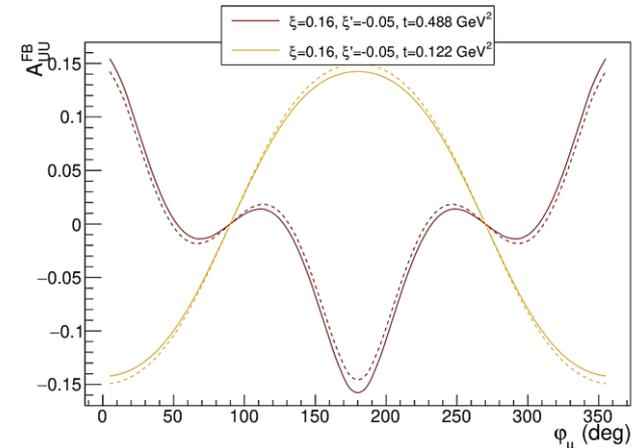
$$A_{UU}^{\mu\pm}(\varphi_\mu) = \frac{d^5\Sigma_{UU}(\varphi_{\mu-}) - d^5\Sigma_{UU}(\varphi_{\mu+})}{d^5\Sigma_{UU}(\varphi_{\mu-}) + d^5\Sigma_{UU}(\varphi_{\mu+})}$$

$$= \frac{d^5\Sigma_{BH_{12}} + d^5\Sigma_{\mathcal{I}_2}}{d^5\Sigma_{BH_1} + d^5\Sigma_{BH_2} + d^5\Sigma_{DDVCS} + d^5\Sigma_{\mathcal{I}_1}}$$

$$d^5\Sigma_{\mathcal{I}_2} \propto -\frac{\xi'}{\xi} \Re \left[F_1 \mathcal{H} + \frac{\xi^2}{\xi'} (F_1 + F_2) \tilde{\mathcal{H}} - \frac{t}{4M_N^2} F_2 \mathcal{E} \right]$$

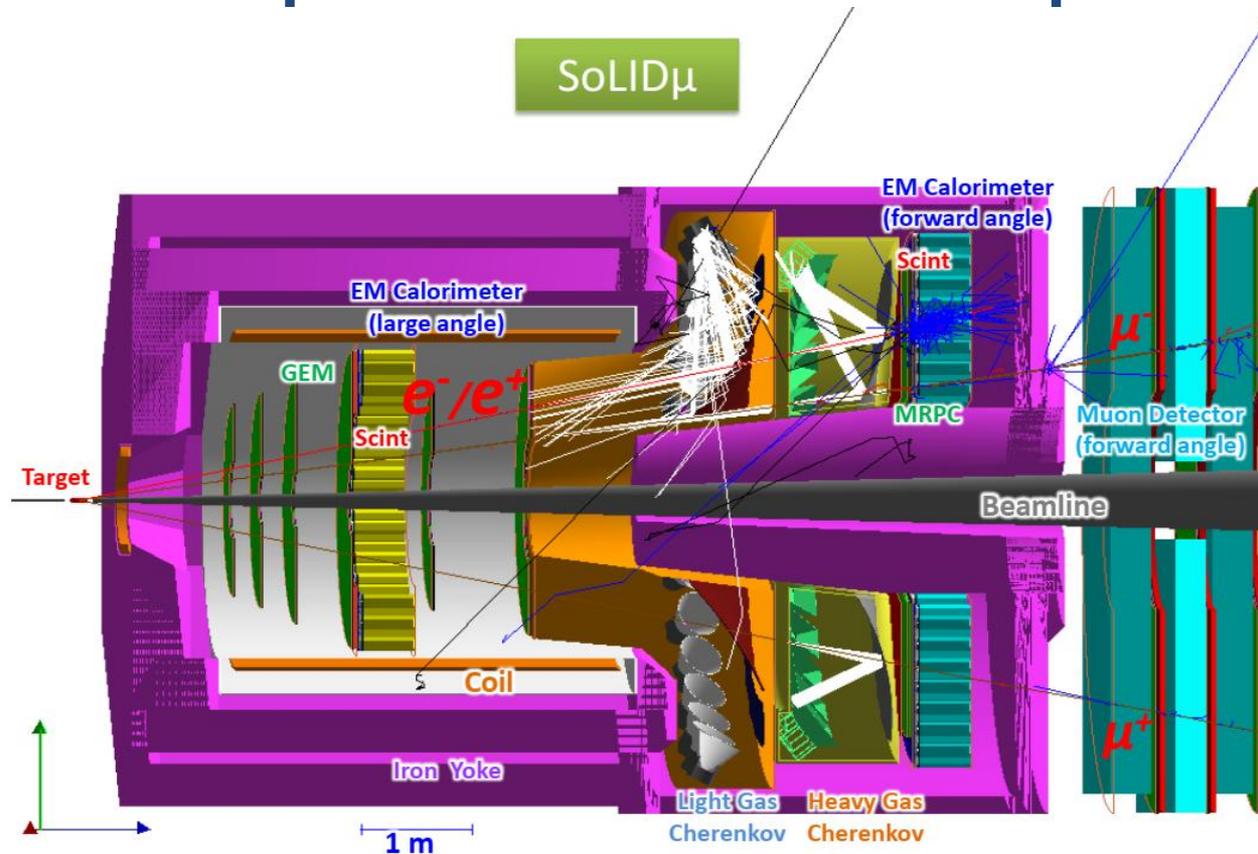
aka Forward Backward Asymmetry

μ CA in two regions



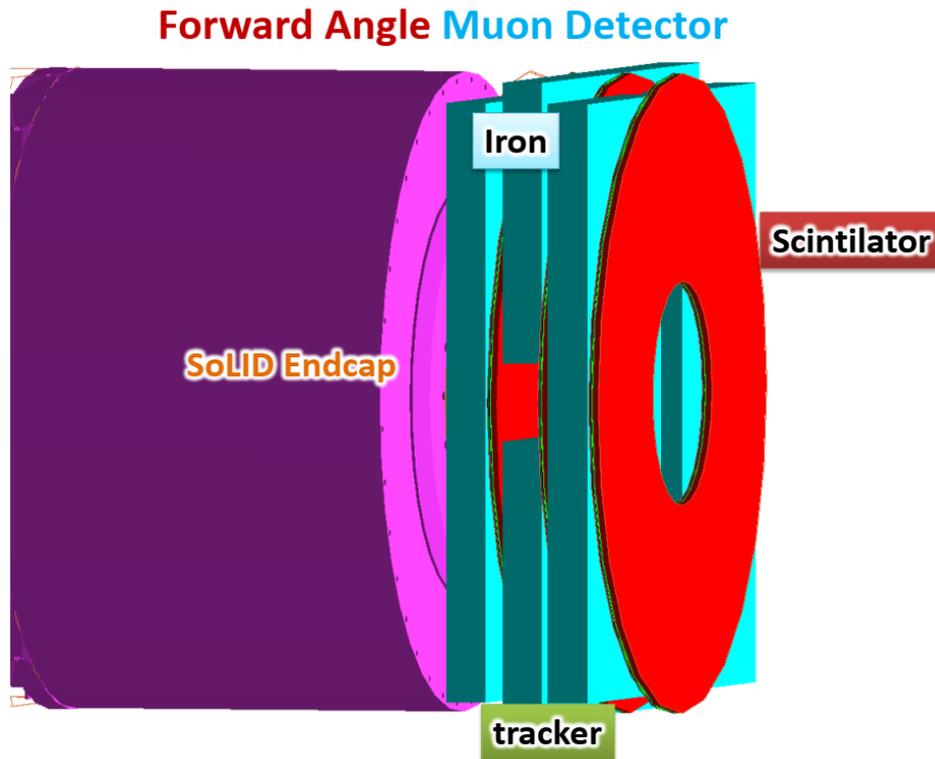
- Access to the real part of CFFs (no dispersion relation has been established)
- **μ CA** predicted to have **significant amplitude** and rich **harmonic composition**, like the forward-backward asymmetry of TCS
- **Curvature change** is a highly-discriminating feature for models
- **DDVCS μ CA** access a CFF combination **different from BSA**. This feature **distinguishes DDVCS** from DVCS and TCS.

Experimental Setup



- SoLID can detect e^- , e^+ , proton, pion
- Based on SoLID J/Psi and TCS setup ($1.2e37/cm^2/s$) with forward angle muon detector added to form SoLIDμ spectrometer
- Sharing beam time with approved J/Psi and TCS di-e experiment
- Forward Angle (FA) covers 8.5-16.5deg and Large Angle (LA) covers 18-30deg

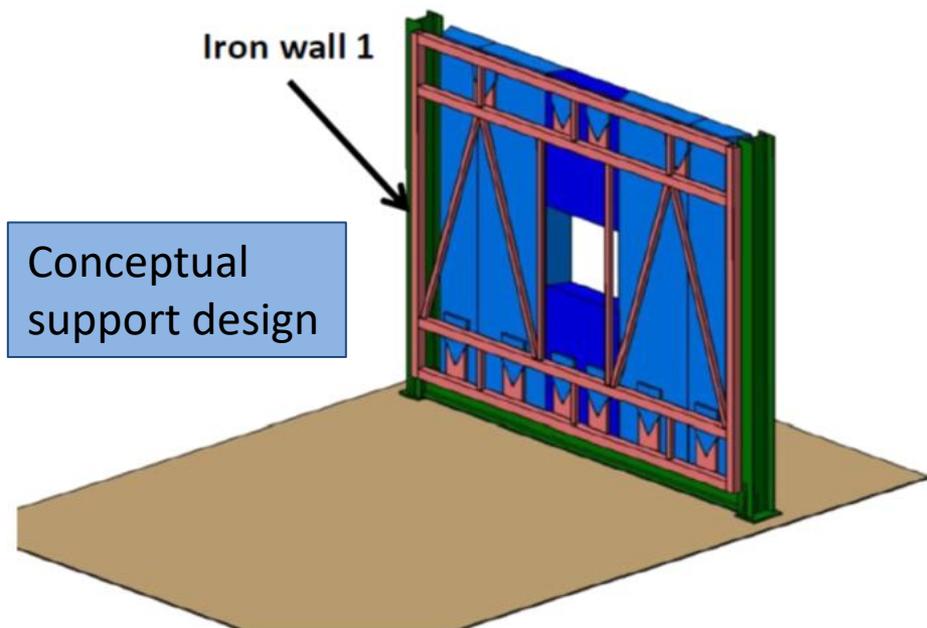
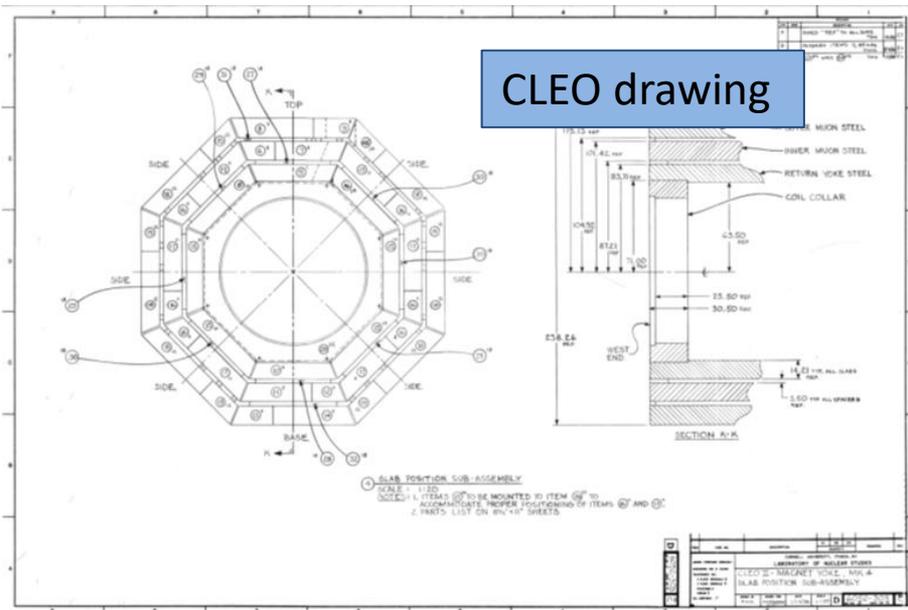
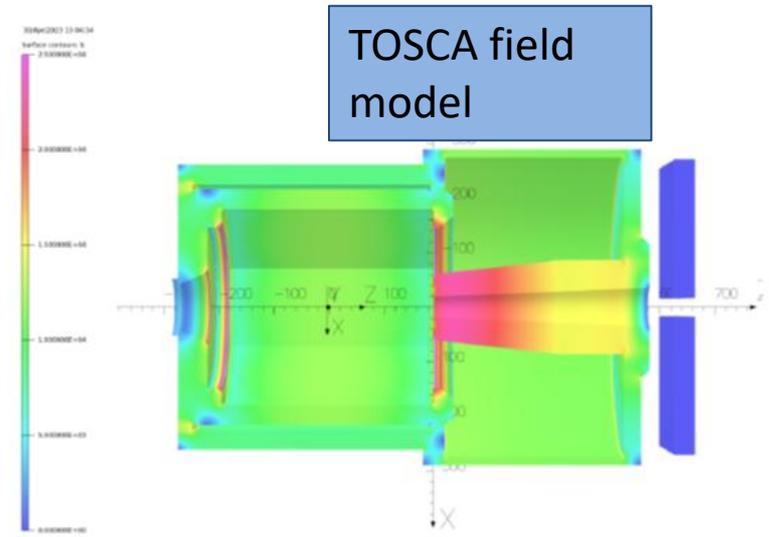
Forward Angle Muon Detector (FAMD)



- 3 layers of iron+tracker+scintillator ($R_{in}=1\text{m}$, $R_{out}=3\text{m}$)
- Iron for pion blocking
- μ RWell trackers to connect with tracks in SoLID inner GEM trackers
 - track resolution from SoLID inner trackers only
- scintillators for muon PID with pion suppression and trigger

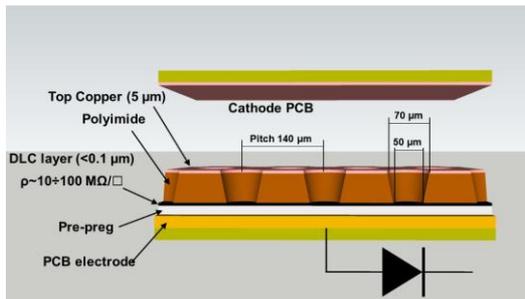
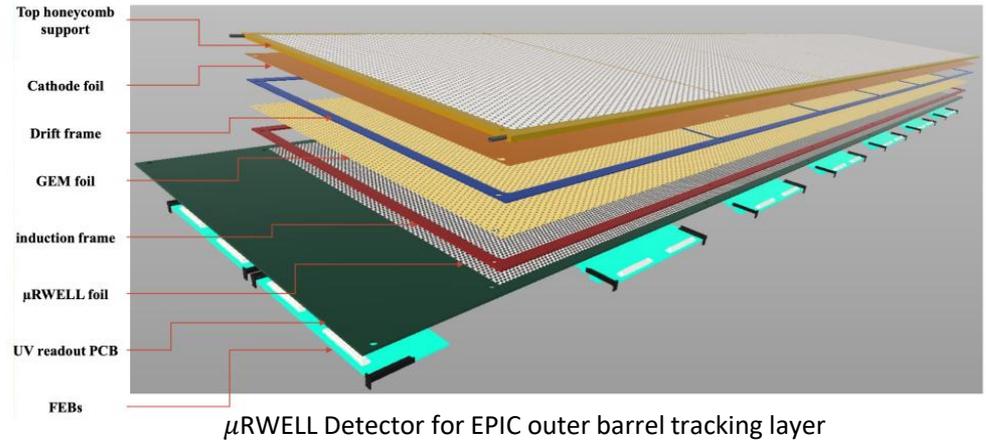
Iron of FAMD

- Reuse 6 of CLEO octagon outer layer iron
- Each one is about 36x254x533cm
- No problem with space
- Field (<10G), force (<1N), torque (<2Nm) are small

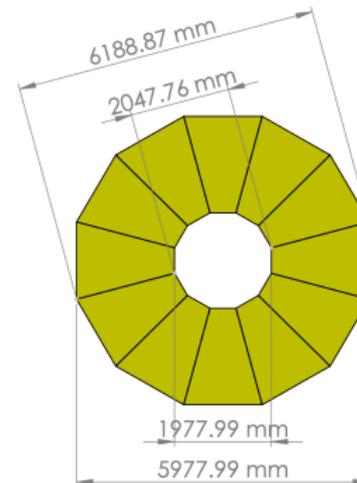


μ RWell trackers of FAMMD

- μ RWell tracker with good rate capability and lower cost than GEM
- VMM electronics for readout
- 2D UV strips with capacitive charge sharing to have rate 30KHz/cm² and position resolution of 1 mm



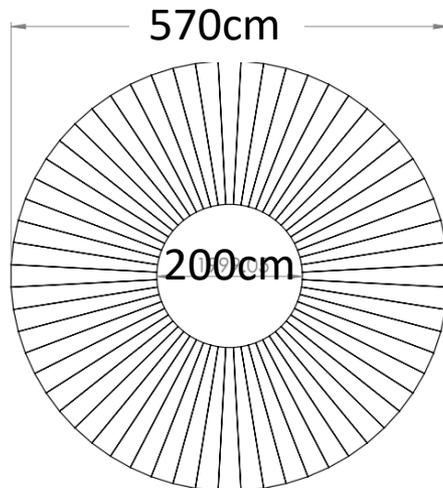
μ RWELL Detector – G. Bencivenni *et al* 2019 *JINST* **14** P05014



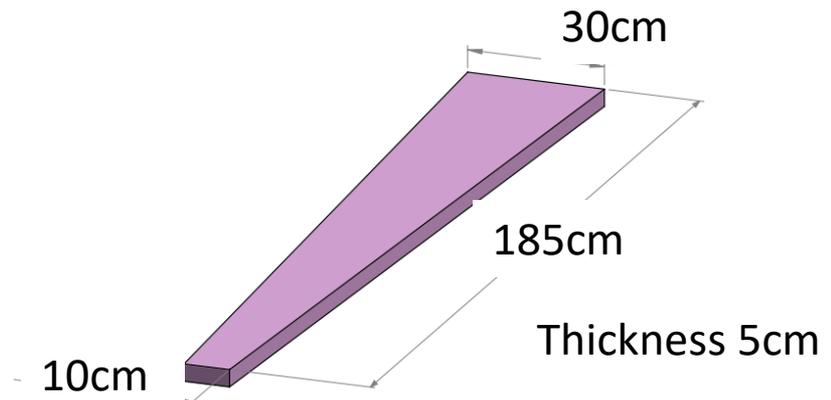
A plane of μ RWELL detector

Scintillators of FAMD

- 3 layers of scintillator planes
- Each plane has 60 azimuthal segments
- Readout with light guide and PMTs from both inner and outer radial ends
- Design similar to CLAS12 forward scintillator and SoLID large angle scintillator with similar performance



A plane of scintillator detector



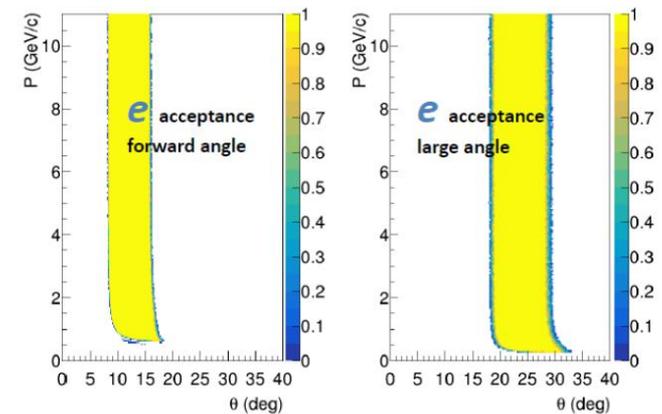
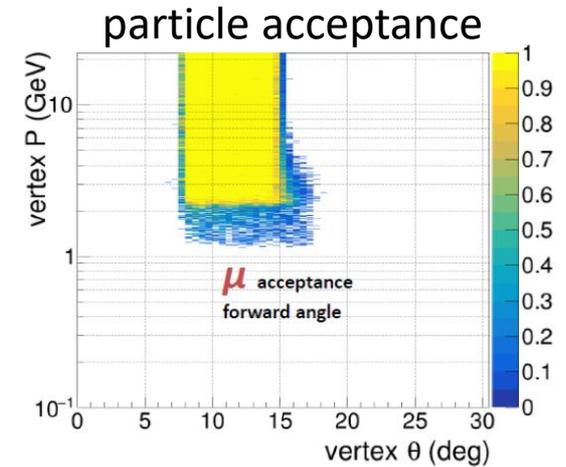
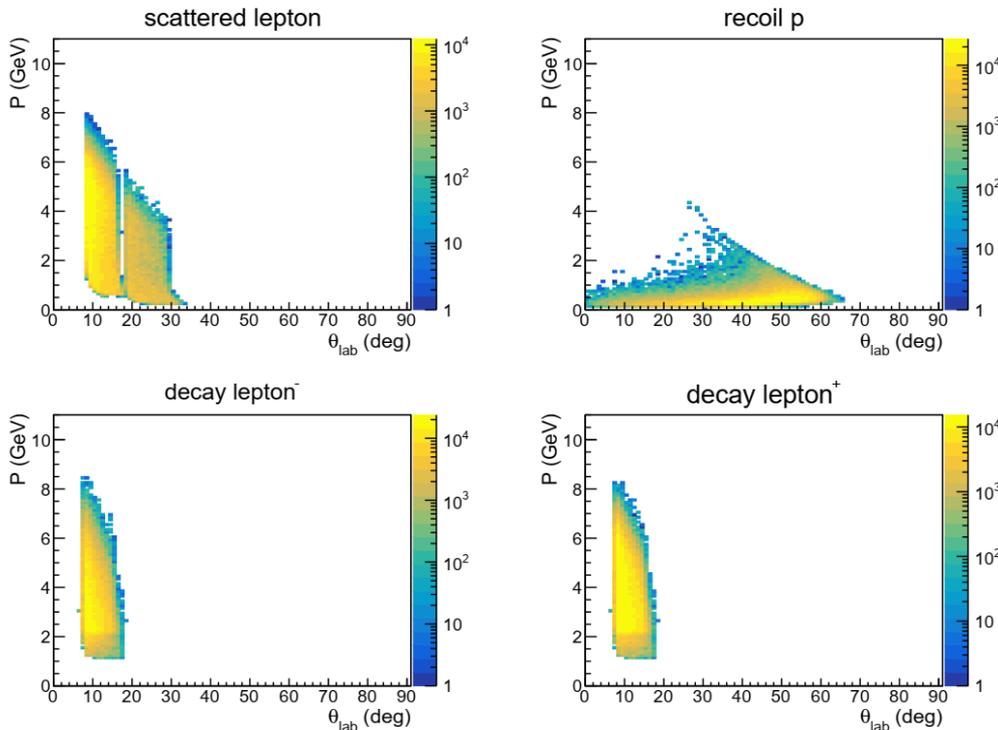
A module of scintillator detector

Event Acceptance

BH generator "grape-dilepton" used by HERA and verified by CLAS12

- Best topology 3-fold(e+mu+mu): scattered e- at FA+LA, both muons at FA, proton not detected
- Additional topology 4-fold(e+mu+mu+p): recoil proton at FA+LA (clean)

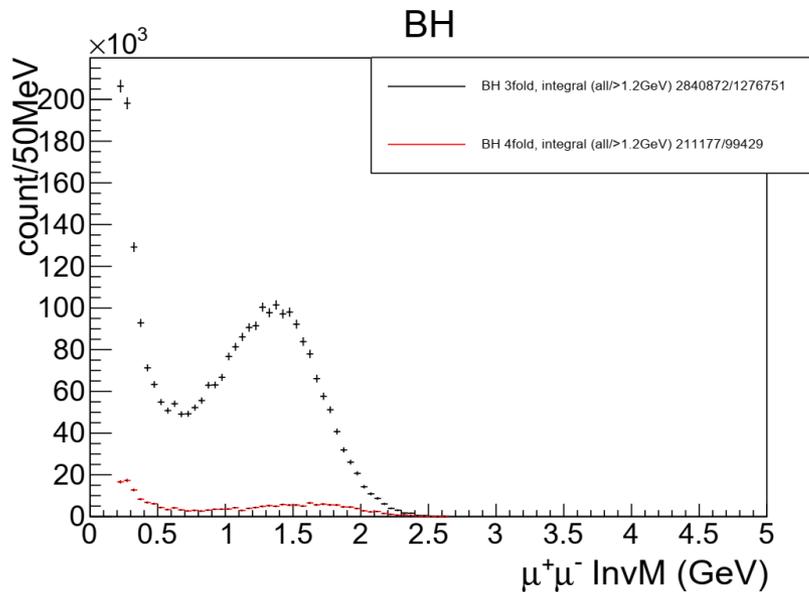
accepted BH 3-fold events



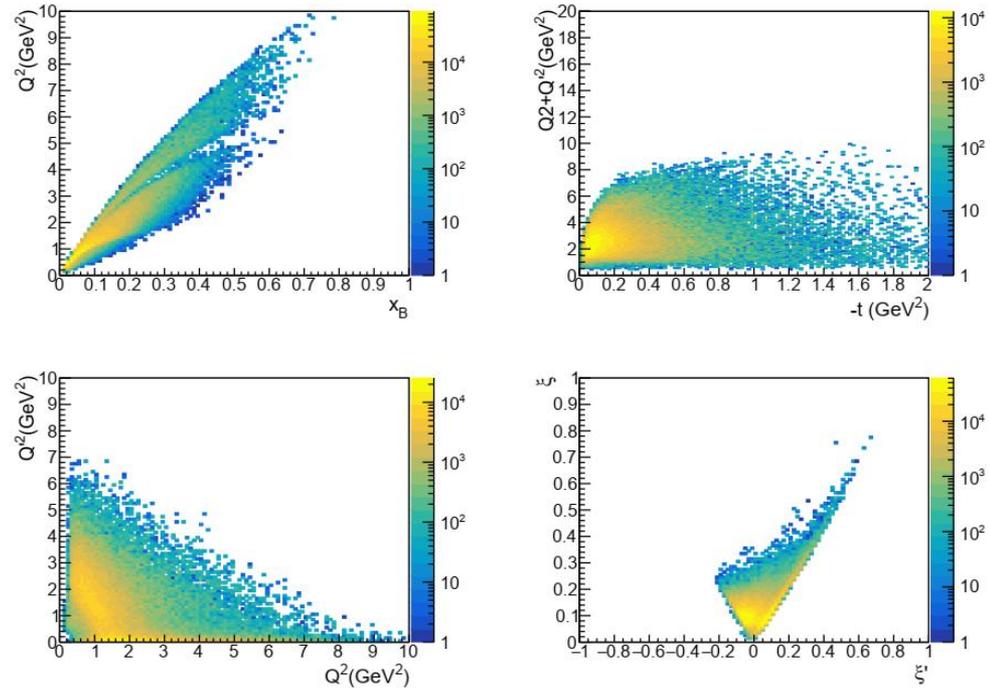
- full azimuthal coverage and large acceptance
- Solenoid field helps control systematics

Event Distribution

- 3-fold BH events covers a large kinematic range
- 0.7 overall detection efficiency
- **Enough counts** with $1.2e37/cm2/s$ luminosity and 100 days to have **multidimensional binning**

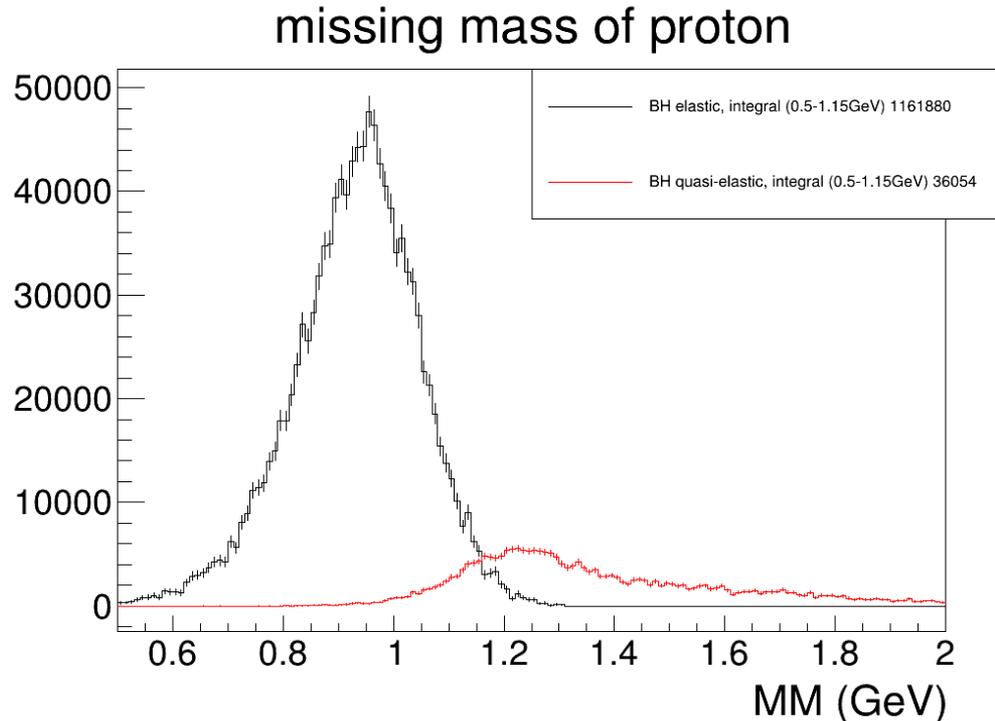


accepted BH 3-fold events



Exclusivity cut

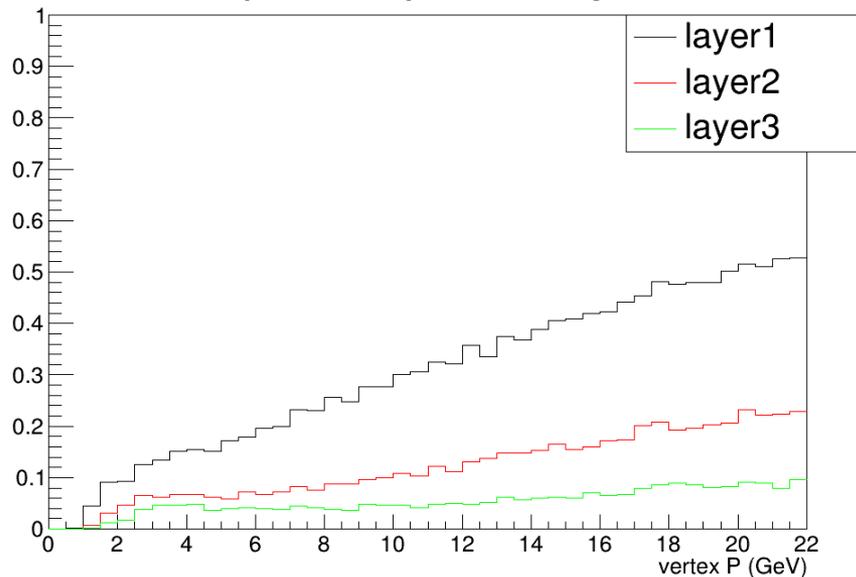
- Both BH with 4 final particles (elastic) and more than 4 particles (quasi-elastic), generated by "grape-dilepton"
- Missing proton mass of 3 fold BH events with resolution from SoLID inner GEM trackers, for resonance free region (muon pair $\text{InvM} > 1.2 \text{ GeV}$)
- 3-4% background after cutting $\text{MM} > 1.15 \text{ GeV}$



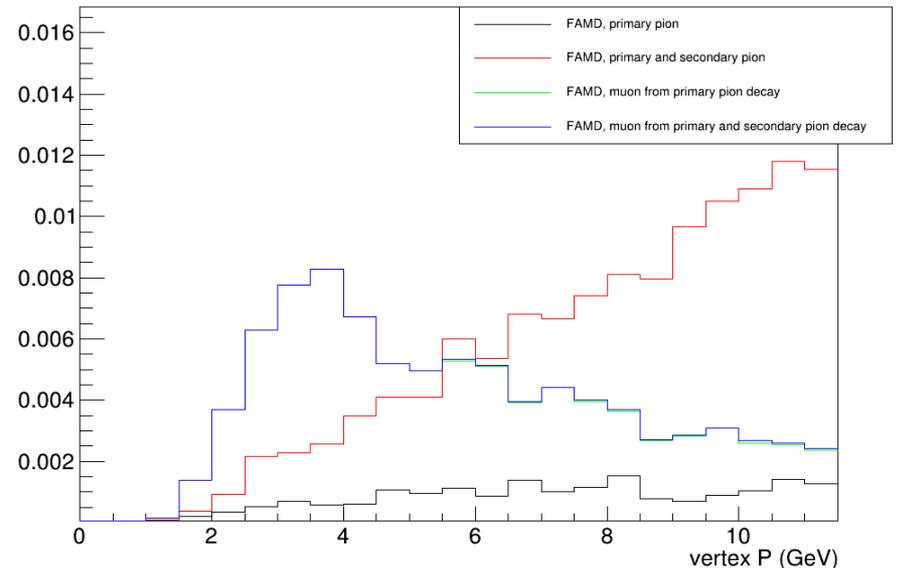
Pion blocking

- Geant4 simulation of pions from target with some probabilities creating hits at FAMD
- "pion hit probability", hits of charged particles entering each layer, used for FAMD background and trigger rate estimate
- "pion surviving probability", hits of pion and muon at the last layer of FAMD with tracks passing all SoLID inner GEM trackers, used for physics event rate estimation

pion hit probability

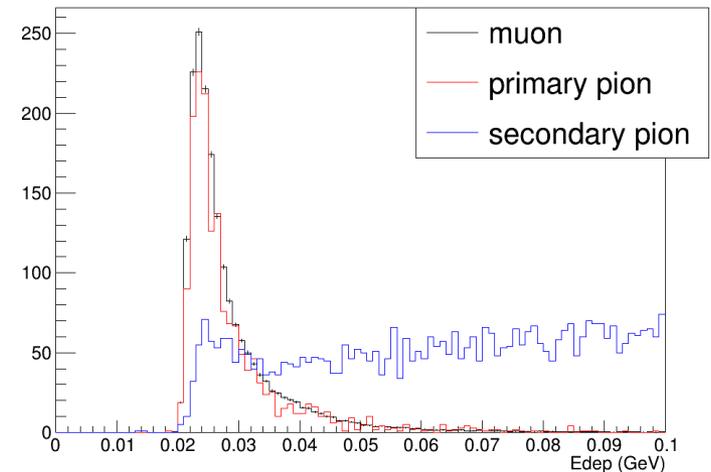
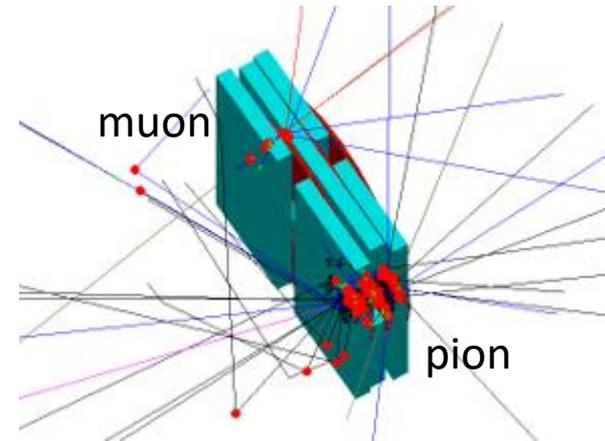


pion surviving probability



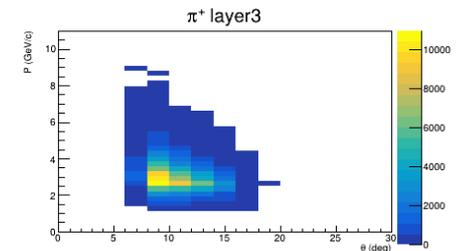
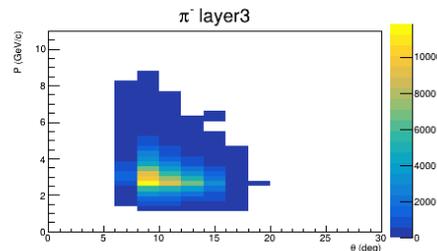
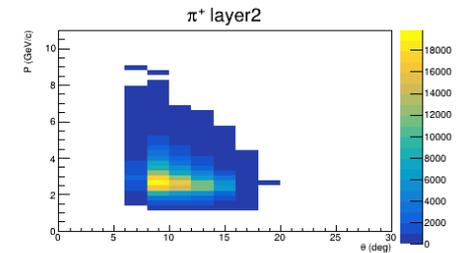
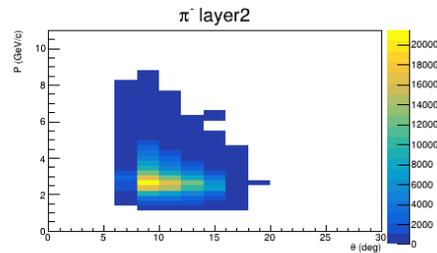
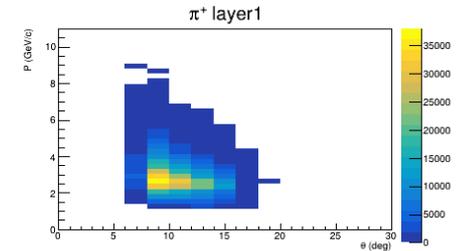
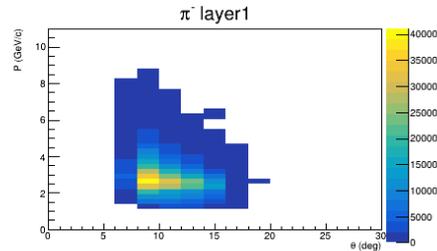
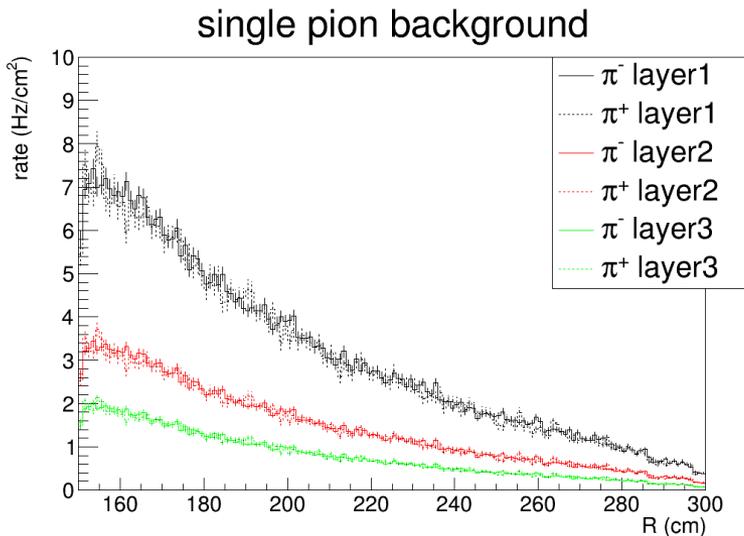
Pion suppression within FAMD

- Muons behave as Minimum Ionizing Particle (MIP)
- Pions often deposit more energy over 3 layers of scintillators.
- Use a moderate pion **suppression factor 2** from energy cut



Single pion background

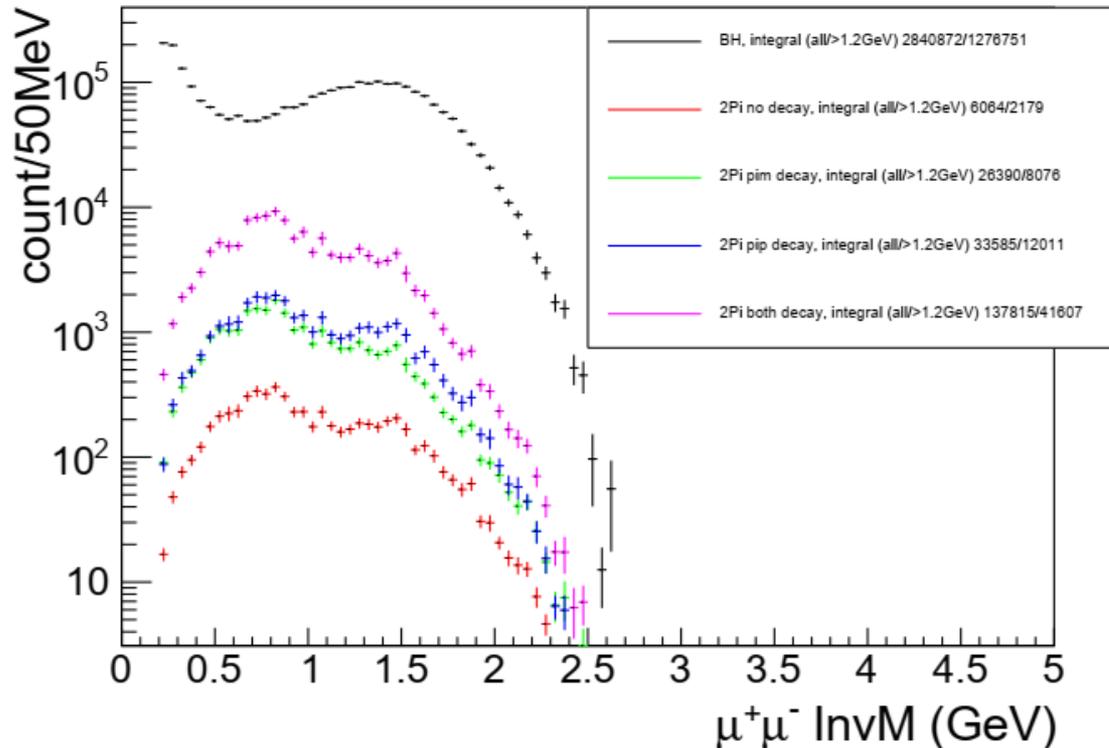
- Combining single pion generator "evgen_bggen" (pythia+MAID) events with "pion hit probability", study charged particle rate at 3 layers. Full simulation confirmed the result
- Single particle trigger 600khz rate with hits in all 3 layers of scintillators in nearby phi sectors
- Coincidence of two hits from 2 single particle trigger from 2 different phi sectors within 50ns time windows leads to **18khz final trigger rate**
- Fake coin rate from single pion is below 1khz. BH di-muon events have two muons separated at least by 60 degrees in phi angle for the main physics region (muon pair $InvM > 1.2 GeV$)



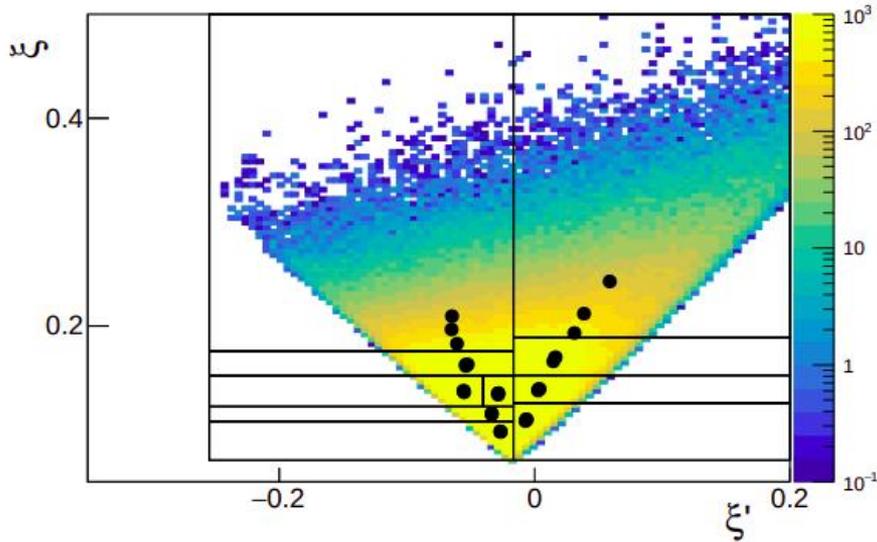
Two pion exclusive background

- Main physics background from two pion exclusive channel (missing mass cut won't reject it because pions and muons have similar mass)
- Combine event generator "twopeg" (fit to CLAS data) and "pion hit probability" with pion suppression factor 2, study "2pi" rate and compare to BH rate
- **5-7% background**, while the channel be measured by the internal SOLID detector at the same time to control systematics

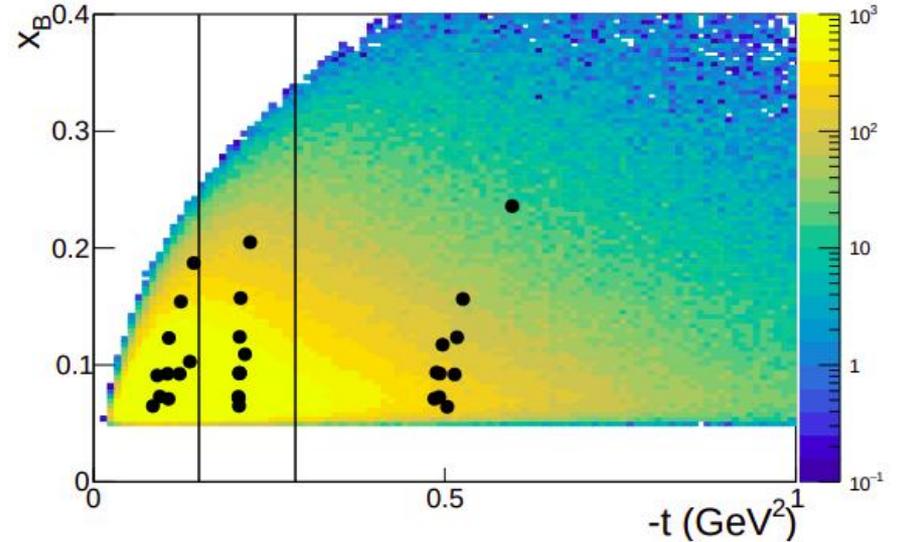
BH and 2pi comparison



Experimental projection binning



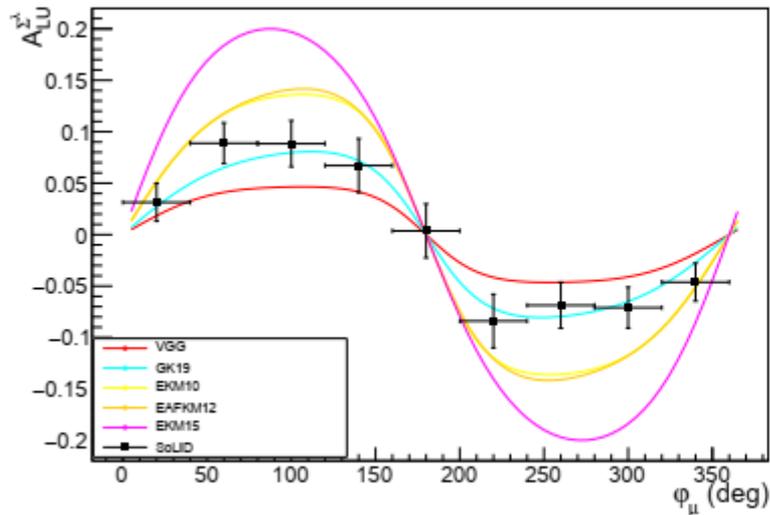
(a) (ξ', ξ) space.



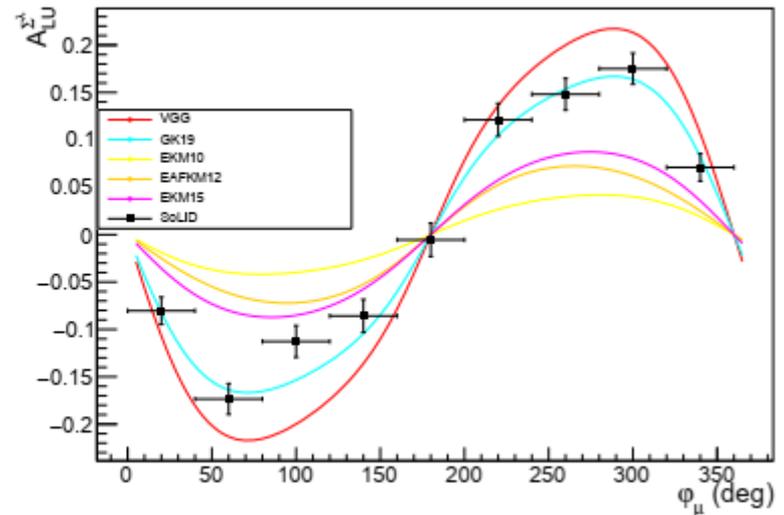
(b) $(-t, x_B)$ space.

- 100 days would allow for measurements on a five-dimensional grid $(\xi' \ \xi \ t \ x_B \ \Phi_\mu)$
- Covers both DVCS-like region ($\xi' > 0, Q^2 > Q'^2$) to TCS-like region ($\xi' < 0, Q^2 < Q'^2$)

BSA experimental projections



DVCS-like region



TCS-like region

arXiv:2502.02346

- **First time measurement** of the **BSA sign change** between the two regions
- Possibility to constrain GPD models

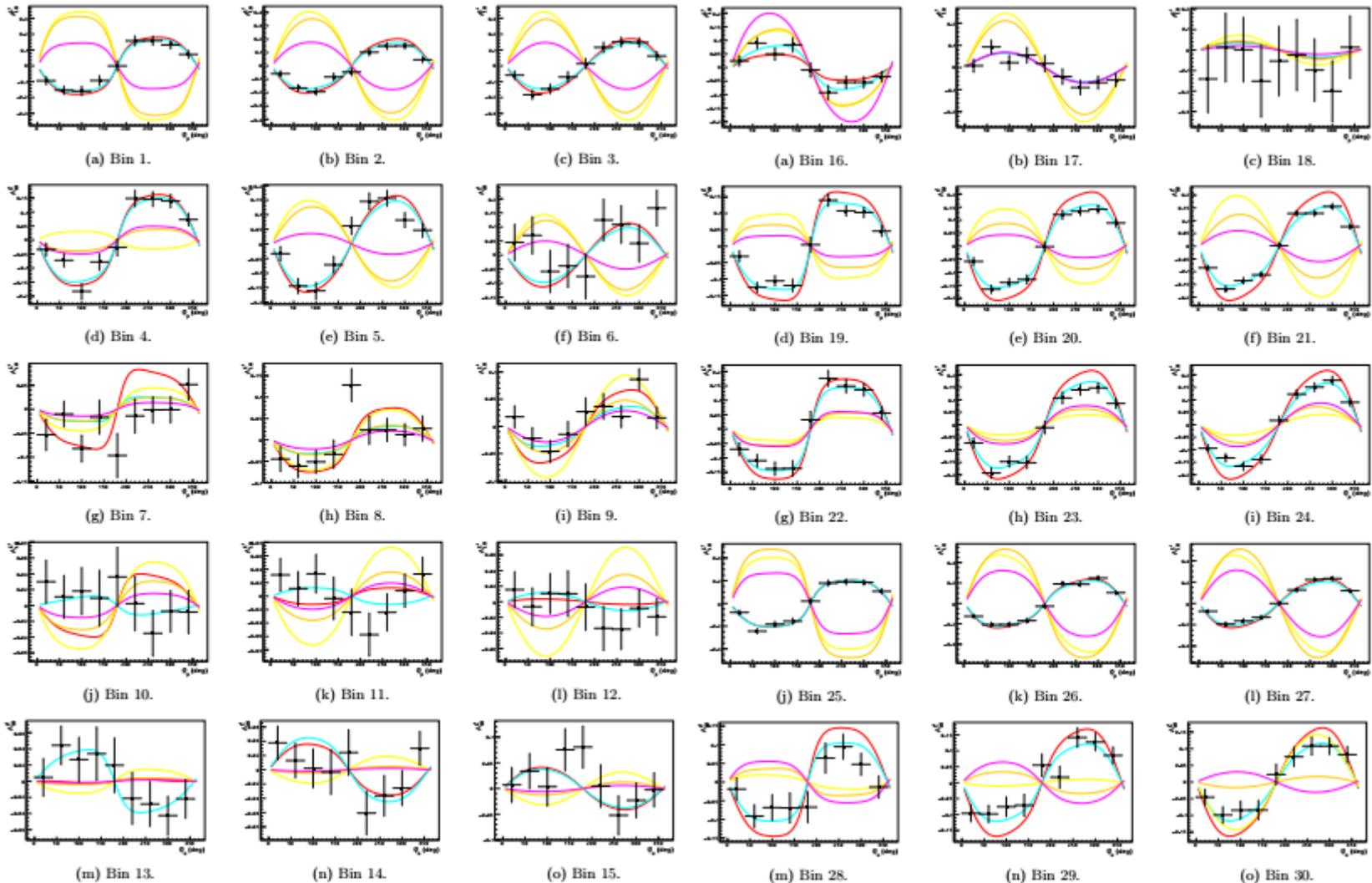
All projection plots include statistical and polarization errors

BSA experimental projections

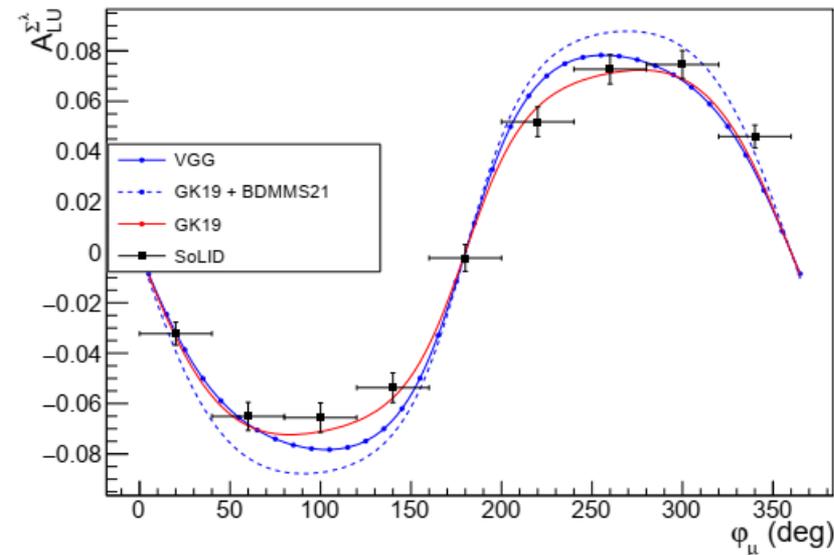
All plots over the entire kinematic range

Bin	ζ' range	ζ range	t range (GeV ²)
1	$-0.255 < \zeta' < 0$	$0.152 < \zeta < 0.176$	$-5.541 < t < -0.287$
2			$-0.287 < t < -0.150$
3			$-0.150 < t < -0.020$
4		$0.176 < \zeta < 0.189$	$-5.541 < t < -0.287$
5			$-0.287 < t < -0.150$
6			$-0.150 < t < -0.020$
7	$0 < \zeta' < 0.512$	$0.071 < \zeta < 0.126$	$-5.541 < t < -0.287$
8			$-0.287 < t < -0.150$
9			$-0.150 < t < -0.020$
10		$0.126 < \zeta < 0.153$	$-5.541 < t < -0.287$
11			$-0.287 < t < -0.150$
12			$-0.150 < t < -0.020$
13		$0.153 < \zeta < 0.189$	$-5.541 < t < -0.287$
14			$-0.287 < t < -0.150$
15			$-0.150 < t < -0.020$
16		$0.189 < \zeta < 0.739$	$-5.541 < t < -0.287$
17			$-0.287 < t < -0.150$
18			$-0.150 < t < -0.020$
19	$-0.255 < \zeta' < -0.017$	$0.071 < \zeta < 0.108$	$-5.541 < t < -0.287$
20			$-0.287 < t < -0.150$
21			$-0.150 < t < -0.020$
22		$0.108 < \zeta < 0.132$	$-5.541 < t < -0.287$
23			$-0.287 < t < -0.150$
24			$-0.150 < t < -0.020$
25	$-0.355 < \zeta' < -0.040$	$0.122 < \zeta < 0.152$	$-5.541 < t < -0.287$
26			$-0.287 < t < -0.150$
27			$-0.150 < t < -0.020$

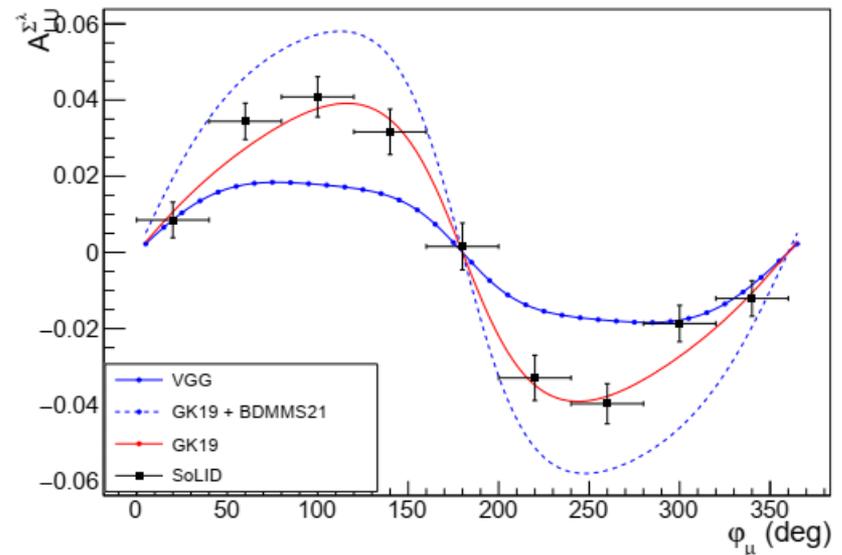
$t < \zeta' < -0.017$ $0.122 < \zeta < 0.152$ $-5.541 < t < -0.287$
 Bin boundaries of the binning scheme shown in Fig. 2



BSA experimental projections



(a) $-0.1 < \xi' < -0.04$.

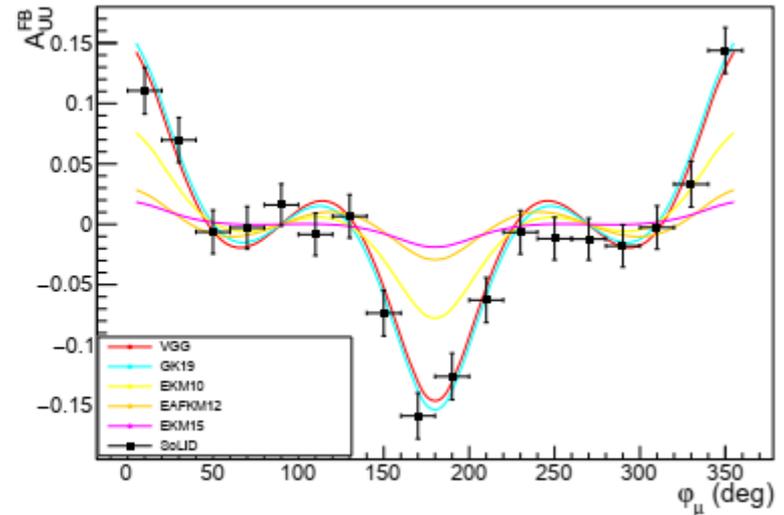
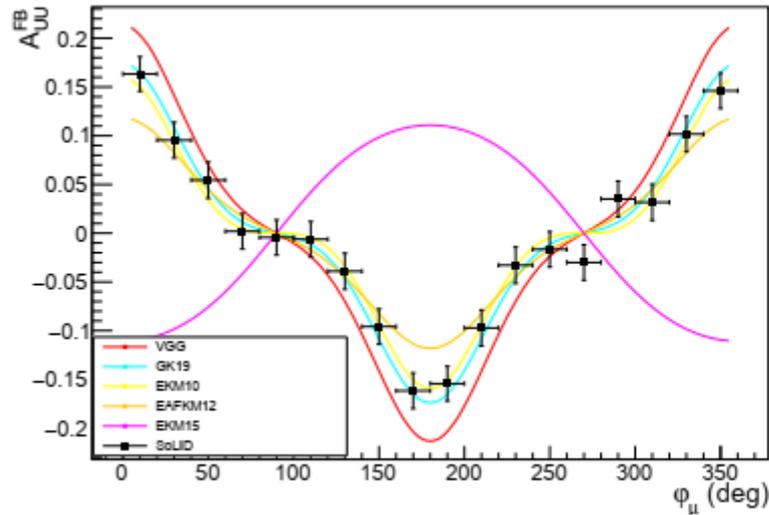


(b) $-0.04 < \xi' < 0.1$.

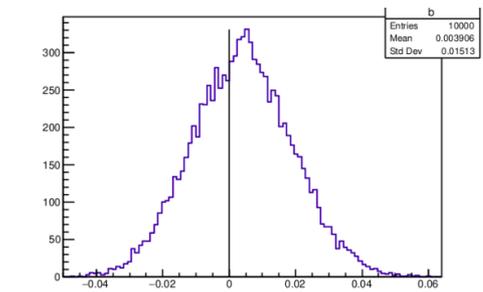
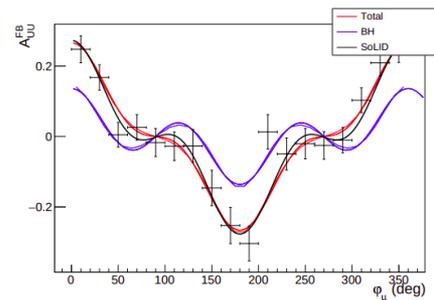
Figure 26: Projected exploratory TCS-like BSA measurements sensitive to shadow GPDs in the $0.3 < \xi < 0.4$ region.

First time exploratory measurement of BSA constraining shadow GPD models (a class of functions with null CFF and forward limit contributing to GPD solutions in the deconvolution problem)

μ CA experimental projections



First time exploratory measurement of μ CA to access the CFF real part with curvature change



(a) μ CA and the components entering the $\cos \varphi_\mu$ mo-

(b) Distribution of the $\cos \varphi_\mu$ moment of the μ CA

$$A_{UU}^{\mu\pm}(\varphi_\mu) = a_0 + a_1 \cos(\varphi) + a_3 \cos(3\varphi).$$

- known BH contribution is small in certain regions and can be subtracted
- μ CA has contributions from $\cos(\phi)$ and $\cos(3\phi)$ modulations
- $\cos(\phi)$ component can be extracted from fitting

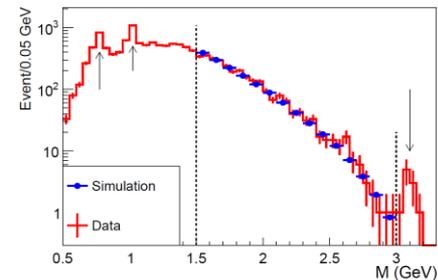
Systematic effects

BSA systematics originates mainly from electron beam polarization, electron detection efficiency, and muon detection efficiency

$$A_{LU}^{\Sigma\lambda} = \frac{1}{\lambda} \frac{Y_+ - Y_-}{Y_+ + Y_-} \quad Y_{\pm}(\varphi_{\mu}) = \frac{1}{Q_{\pm}} \frac{1}{\Delta\Omega_e(\varphi_{\mu}) \Delta\theta_{\mu}(\varphi_{\mu})} \int_0^{2\pi} d\phi \int_{\pi/4}^{3\pi/4} d\theta_{\mu} \sin(\theta_{\mu}) \frac{N_{\pm}(\varphi_{\mu}, \phi, \theta_{\mu})}{\epsilon_e(\phi) \epsilon_{\mu}(\varphi_{\mu}, \theta_{\mu})}$$

$$Y_{\pm}(\varphi_{\mu}) \equiv \sum_{i=1}^{N_{\phi}} \sum_{j=1}^{N_{\theta_{\mu}}} \frac{n_{\pm}^{ij}}{\epsilon_e^i \epsilon_{\mu}^j} \quad \delta A_{LU}^{\Sigma\lambda} = \sqrt{\left[A_{LU}^{\Sigma\lambda}\right]^2 \left(\frac{\delta\lambda}{\lambda}\right)^2 + \frac{1}{2\lambda^2} \frac{1}{N_{\phi}} \left(\frac{\delta\epsilon_e}{\epsilon_e}\right)^2 + \frac{1}{2\lambda^2} \frac{1}{N_{\theta_{\mu}}} \left(\frac{\delta\epsilon_{\mu}}{\epsilon_{\mu}}\right)^2} \quad \lambda = 0.85 \rightarrow 0.04$$

Bin independence hypothesis ($N_{\phi}, N_{\theta_{\mu}}$) are the kinematic dependent number of bins, typically (20,10)



CLAS12 BH di-e data and sim comparison

Control systematics through reference channels

- SoLID will have crosssection measurement before this experiment
- For e- detection, use inclusive DIS and elastic measurements
- For muon detection, use both resonance and resonance free region and cross check both di-e and di-mu channels
- Pion channel measurement are also taken at the same time

Beam time request

Beam Energy (GeV)	Beam Current (μA)	Beam Requirements	Target Material	Target Thickness (cm)	Beam time (days)
11	3	polarized ($>85\%$)	LH2	15	
Run Group Calibration time					10
Run Group Production time					50
Requested Production time					50
Total Time					110

- Main trigger on di-muon to take DDVCS, J/psi and TCS di-mu data at the same time
- Independent di-e trigger for approved J/psi and TCS di-e data taking at the same time
- **Comprehensive program including muons and electrons within same runs.** It can also help cross check systematics

Summary

This proposed experiment

- complement SoLID J/psi setup with a forward angle **muon detector** to form **SoLID μ spectrometer**
- measure **DDVCS** in the di-muon channel
- **share** approved J/psi beamtime 60 days and request **additional 50 days**

Its physics impact

- **first time measurement** of **DDVCS** (mainly BSA and exploratory μ CA) over a broad kinematic range
- **first time to access GPD** $|x| < \xi$ as input for models and global fitting

Proposal to PAC53 PR12-25-010

Proposal to JLab PAC 53

Double Deeply Virtual Compton Scattering with SoLID μ spectrometer

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and SoLID Collaboration

Spokesperson : Juan-Sebastian Alvarado, Alexandre Camsonne, Marie Boer,
Eric Voutier, Xinzhan Bai, Zhiwen Zhao

Backup

GPD Parameterization

- **GPDs are universal quantities and reflect nucleon structure independently of the probing reaction.**

- At leading twist–2, four quark chirality conserving GPDs for each quark type and gluon.

$H^{q,g}(x, \xi, t)$
spin avg
no hel. flip

$E^{q,g}(x, \xi, t)$
spin avg
helicity flip

- Because quark helicity is conserved in the hard scattering regime, the produced meson acts as a helicity filter.

$\tilde{H}^{q,g}(x, \xi, t)$
spin diff
no hel. flip

$\tilde{E}^{q,g}(x, \xi, t)$
spin diff
helicity flip

- **Need a variety of Hard Exclusive Measurements to disentangle the different GPDs.**

Compton Scattering:

- Sensitive to all four GPDs.

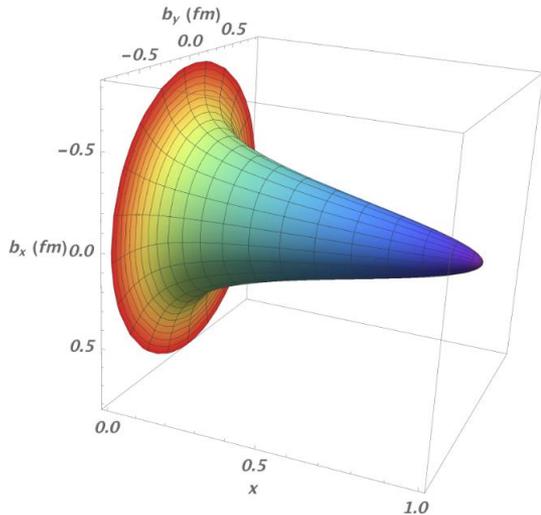
Deep Exclusive Meson Production:

- Vector mesons sensitive to spin–average $H E$.
- Pseudoscalar sensitive to spin–difference \tilde{H}, \tilde{E} .

Nucleon Femtography

M. Burkardt PRD 62 (2000) 071503. M. Diehl EPJC 25 (2002) 223 A.V. Belitsky, D. Müller, NPA 711 (2002) 118c J.P. Ralston; B. Pire PRD 66 (2002) 111501

$$\rho_H^q(x, \mathbf{b}_\perp) = \int \frac{d^2 \Delta_\perp}{(2\pi)^2} e^{i\mathbf{b}_\perp \cdot \Delta_\perp} [H^q(x, 0, -\Delta_\perp^2) + H^q(-x, 0, -\Delta_\perp^2)]$$



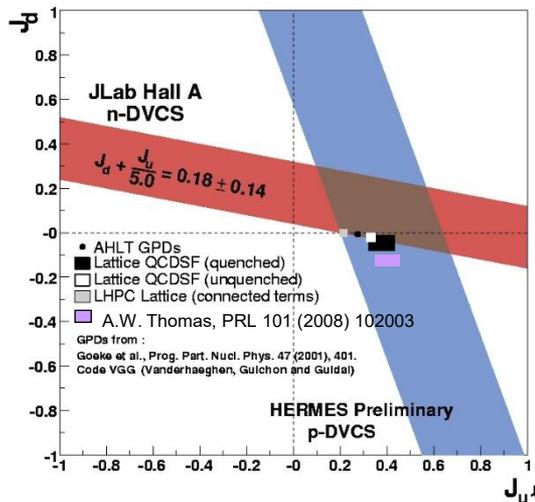
- The **transverse densities** of partons in nucleons and nuclei is related to the transverse momentum transfer ($-\Delta_\perp^2$) dependence of GPDs at **zero-skewness**.
- **DVCS** and **TCS** cannot map out **zero-skewness GPDs** over the **full physics phase space**.

The **experimental knowledge** of the **ξ -dependence** of GPDs at fixed longitudinal momentum fraction allows to **control** the **zero-skewness extrapolation** required for **nucleon imaging**.

R. Dupré, M. Guidal, M. Vanderhaeghen, PRD 95 (2017) 011501

Nucleon Spin

$$\lim_{t \rightarrow 0} \int_{-1}^1 x [H^q(x, \xi, t) + E^q(x, \xi, t)] dx = J^q$$

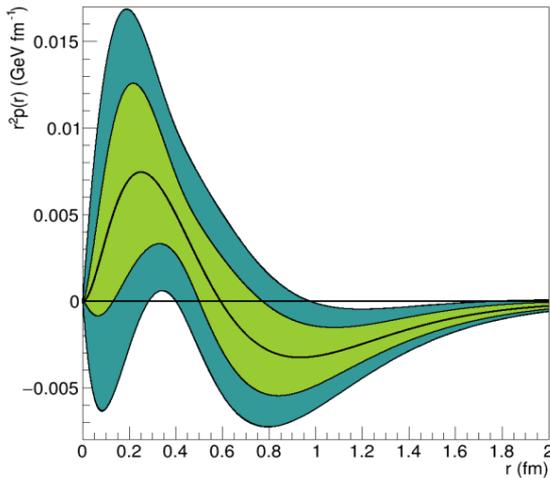


- The **total angular momentum of partons** inside the nucleon can be inferred from the J_i sum rule which involves the **forward limit** of the **first Mellin moment** of partons helicity conserving GPDs.
- **DVCS** and **TCS** cannot access GPDs at $x \neq \xi$ over the **full physics phase space**.

The **experimental knowledge** of the **ξ -dependence** of GPDs at fixed longitudinal momentum fraction is a **mandatory step** for unraveling the **nucleon spin**.

Nucleon Forces

$$\int_{-1}^1 x \sum_q H^q(x, \xi, t) dx = M_2(t) + \frac{4}{5} \xi^2 d_1(t)$$



- The **skewness dependence** of the **first Mellin moment** of the GPD H provides an access to the **gravitational form factors** of the energy momentum tensor of the nucleon.
- **e^\pm -DVCS** and **TCS** offers another path via **dispersion relations**.

The **ξ -dependence** of GPDs reveals the **internal dynamics** of the nucleon.

V. Burkert, L. Elouadrhiri, F.-X. Girod, Nat. 557 (2018) 396; arXiv:2104.02031

Integrated Cross Section

5-fold observables obtained from the **integration over** the **polar angle** of the **muon** and the **azimuthal angle of initial virtual photon or final virtual photon** are required, also **minimizing** the contribution of the **BH₂** process

DVCS-like xs
(integral of ϕ_μ)

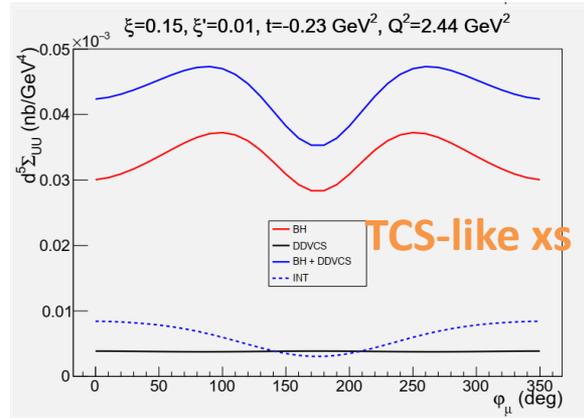
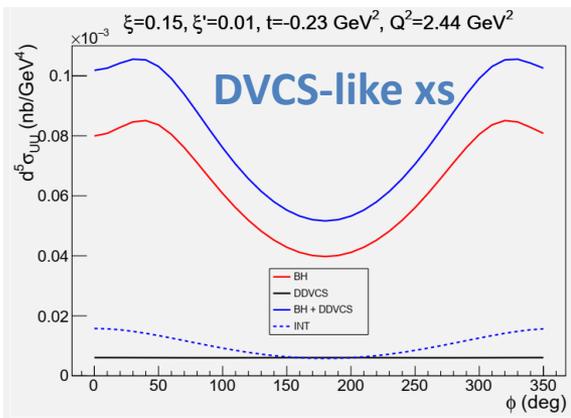
$$d^5\sigma^\lambda(\phi) \equiv \frac{d^5\sigma^\lambda(\phi)}{dx_B dy dt dQ'^2 d\phi} = \int_0^{2\pi} d\varphi_\mu \int_{\pi/2-\theta_0}^{\pi/2+\theta_0} d\theta_\mu \sin(\theta_\mu) \frac{d^7\sigma^\lambda(\phi, \theta_\mu, \phi_\mu)}{dx_B dy dt d\phi dQ'^2 d\Omega_\mu}$$

$$d^5\sigma^\lambda = d^5\sigma_{BH_1} + d^5\sigma_{BH_2} + d^5\sigma_{DDVCS} + d^5\sigma_{\mathcal{I}_1} + \lambda d^5\tilde{\sigma}_{\mathcal{I}_1} = d^5\sigma_{UU} + \lambda d^5\sigma_{LU}$$

TCS-like xs
(integral over ϕ)

$$d^5\Sigma^\lambda(\varphi_\mu) \equiv \frac{d^5\sigma^\lambda(\varphi_\mu)}{dx_B dy dt dQ'^2 d\varphi_\mu} = \int_0^{2\pi} d\phi \int_{\pi/2-\theta_0}^{\pi/2+\theta_0} d\theta_\mu \sin(\theta_\mu) \frac{d^7\sigma^\lambda(\phi, \theta_\mu, \phi_\mu)}{dx_B dy dt d\phi dQ'^2 d\Omega_\mu}$$

$$d^5\Sigma^\lambda = d^5\Sigma_{BH_1} + d^5\Sigma_{BH_2} + d^5\Sigma_{BH_{12}} + d^5\Sigma_{DDVCS} + d^5\Sigma_{\mathcal{I}_1} + d^5\Sigma_{\mathcal{I}_2} + \lambda d^5\tilde{\Sigma}_{\mathcal{I}_2} = d^5\Sigma_{UU} + \lambda d^5\Sigma_{LU}$$



Our study focuses on using **TCS-like xs** for projection

Muon Charge Asymmetry

aka Forward Backward Asymmetry

$$A_{UU}^{FB}(\varphi_\mu) = \frac{d^5\Sigma_{UU}(\varphi_{\mu^-}) - d^5\Sigma_{UU}(\varphi_{\mu^-} + \pi)}{d^5\Sigma_{UU}(\varphi_{\mu^-}) + d^5\Sigma_{UU}(\varphi_{\mu^-} + \pi)} = \frac{d^5\Sigma_{UU}(\varphi_{\mu^-}) - d^5\Sigma_{UU}(\varphi_{\mu^+})}{d^5\Sigma_{UU}(\varphi_{\mu^-}) + d^5\Sigma_{UU}(\varphi_{\mu^+})} = A_{UU}^{\mu^\pm}(\varphi_\mu)$$

$$\begin{aligned} d^5\Sigma_{UU}(\varphi_{\mu^-} + \pi) &= \int_0^{2\pi} d\phi \int_{\pi/2-\theta_0}^{\pi/2+\theta_0} d\theta_{\mu^-} \sin(\theta_{\mu^-}) \frac{d^7\sigma^0(\phi, \pi - \theta_{\mu^-}, \varphi_{\mu^-} + \pi)}{dx_B dy dt d\phi dQ'^2 d\Omega_{\mu^-}} \\ &= \int_0^{2\pi} d\phi \int_{\pi/2-\theta_0}^{\pi/2+\theta_0} d\theta_{\mu^+} \sin(\theta_{\mu^+}) \frac{d^7\sigma^0(\phi, \theta_{\mu^+}, \varphi_{\mu^+})}{dx_B dy dt d\phi dQ'^2 d\Omega_{\mu^+}} = d^5\Sigma_{UU}(\varphi_{\mu^+}) \end{aligned}$$

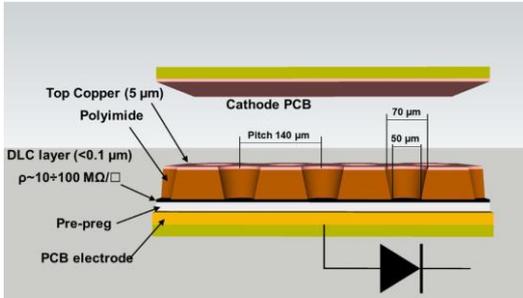
$$A_{UU}^{\mu^\pm}(\varphi_\mu) = \frac{d^5\Sigma_{BH_{12}} + d^5\Sigma_{\mathcal{I}_2}}{d^5\Sigma_{BH_1} + d^5\Sigma_{BH_2} + d^5\Sigma_{DDVCS} + d^5\Sigma_{\mathcal{I}_1}}$$

$$d^5\Sigma_{\mathcal{I}_2} \propto -\frac{\xi'}{\xi} \Re \left[F_1 \mathcal{H} + \frac{\xi^2}{\xi'} (F_1 + F_2) \tilde{\mathcal{H}} - \frac{t}{4M_N^2} F_2 \mathcal{E} \right]$$

- Access to the real part of CFFs (no existing dispersion relation)
- **μCA** predicted to have **significant amplitude** and rich **harmonic composition**, like the forward-backward asymmetry of TCS
- **Curvature change** is a highly-discriminating feature for models
- **DDVCS μCA** access a CFF combination **different** from **BSA**. This feature **distinguishes DDVCS** from DVCS and TCS.

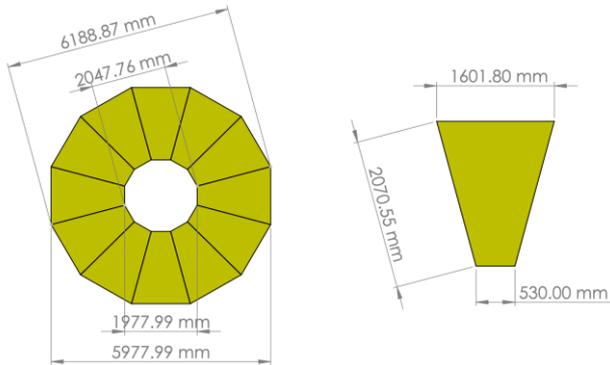
$$A_{UU}^{\mu^\pm}(\varphi_\mu) = a_0 + a_1 \cos(\varphi) + a_3 \cos(3\varphi) \cdot \frac{d^4\sigma_{INT}}{dQ'^2 dt d\Omega} = -\frac{\alpha_{em}^3}{4\pi s^2} \frac{1}{-t} \frac{m_p}{Q'} \frac{1}{\tau\sqrt{1-\tau}} \frac{L_0}{L} \left[\cos(\phi) \frac{1+\cos^2(\theta)}{\sin(\theta)} \text{Re}\tilde{M}^{--} \right. \\ \left. - \cos(2\phi) \sqrt{2} \cos(\theta) \text{Re}\tilde{M}^{0-} + \cos(3\phi) \sin(\theta) \text{Re}\tilde{M}^{+-} + O\left(\frac{1}{Q'}\right) \right],$$

Muon Detector Tracker

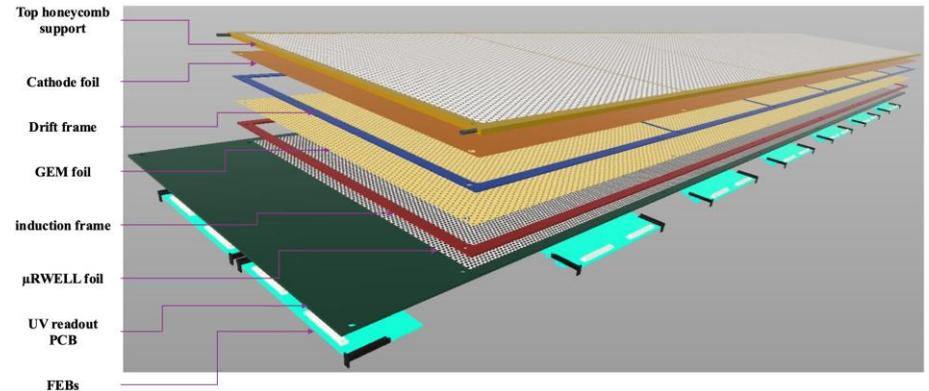


- Utilize μ RWELL detectors for muon tracking layers
 - Current μ RWELL detector rate capability – $\sim 200 \text{ KHz}/\text{cm}^2$ (High-rate version in development – $10 \text{ MHz}/\text{cm}^2$)
 - Discharge resistant thanks to integrated DLC layers – a huge improvement on electronics stability – less interruption on DAQ during running
 - No spacers needed compared with GEM detectors – no dead area
- A similar technology adopted by EIC
 - Our muon detector unit would be roughly in the same size as EIC prototypes
 - Total cost (3 complete layers covering a total of 75 m^2) around 900K

μ RWELL Detector – G. Bencivenni *et al* 2019 *JINST* **14** P05014



A plane of μ RWELL detectors for muon detection



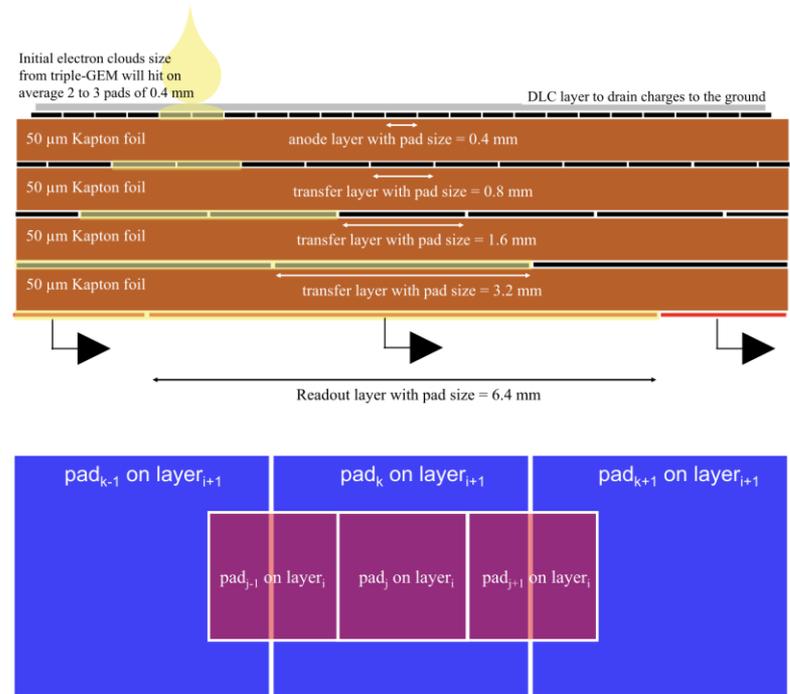
μ RWELL Detector for EPIC outer barrel tracking layer

Muon Detector Tracker

- Use **capacitive charge sharing** technique to reduce total readout channels while maintain the **same space resolution**
- Works for all readout patterns – strip, pad, zigzag, ...

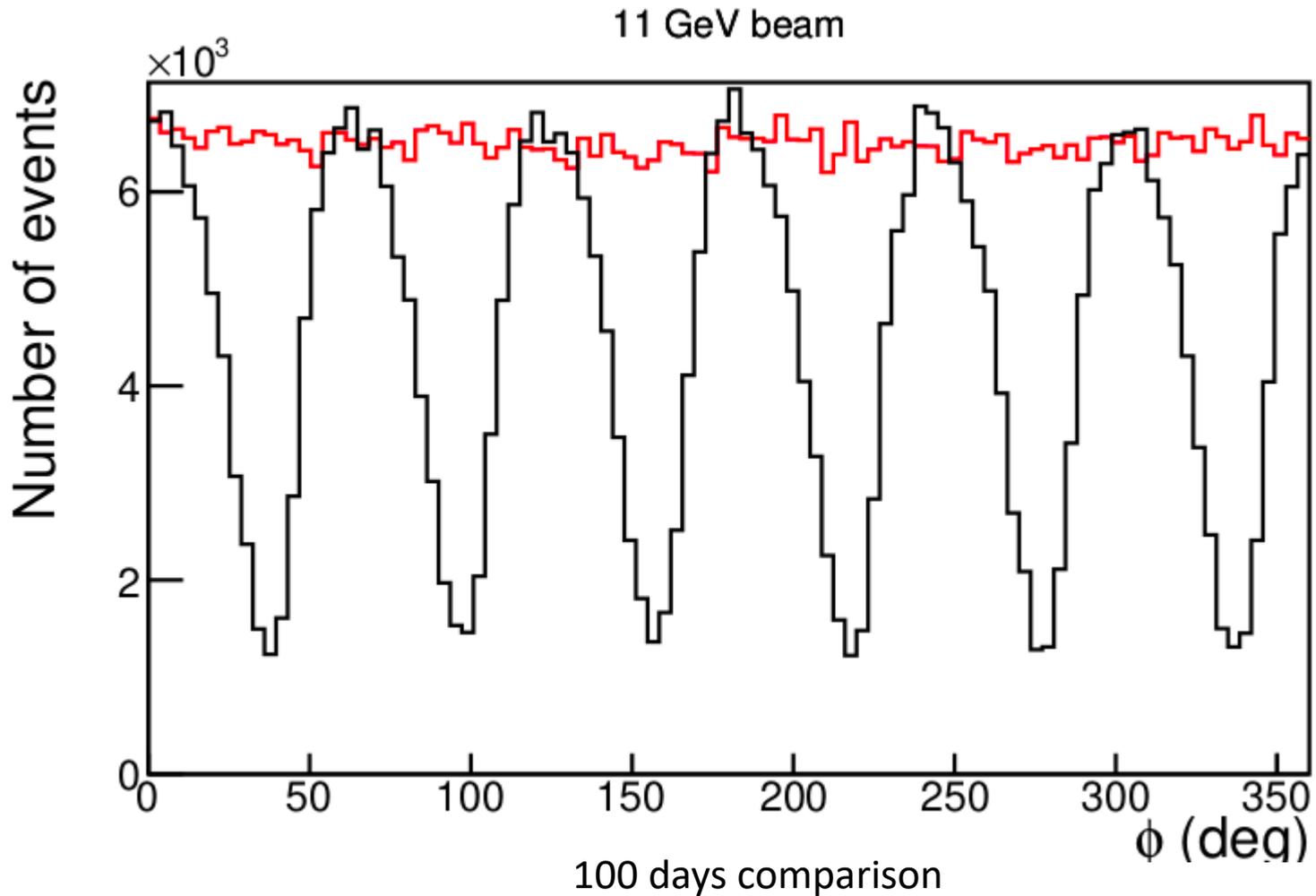
With Capacitive charge sharing:

- Space resolution : 1 mm
- Total readout channel can be reduced to around 22K for all 3 layers combined
- Detector rate will be determined by the final readout strip width, larger strip width leads to lower detector rate capability
- For 22K readout channels, 1 mm space resolution, with capacitive charge sharing technique – **rate capability: $\sim 30 \text{ KHz/cm}^2$** (assume 300 ns signal integral time)

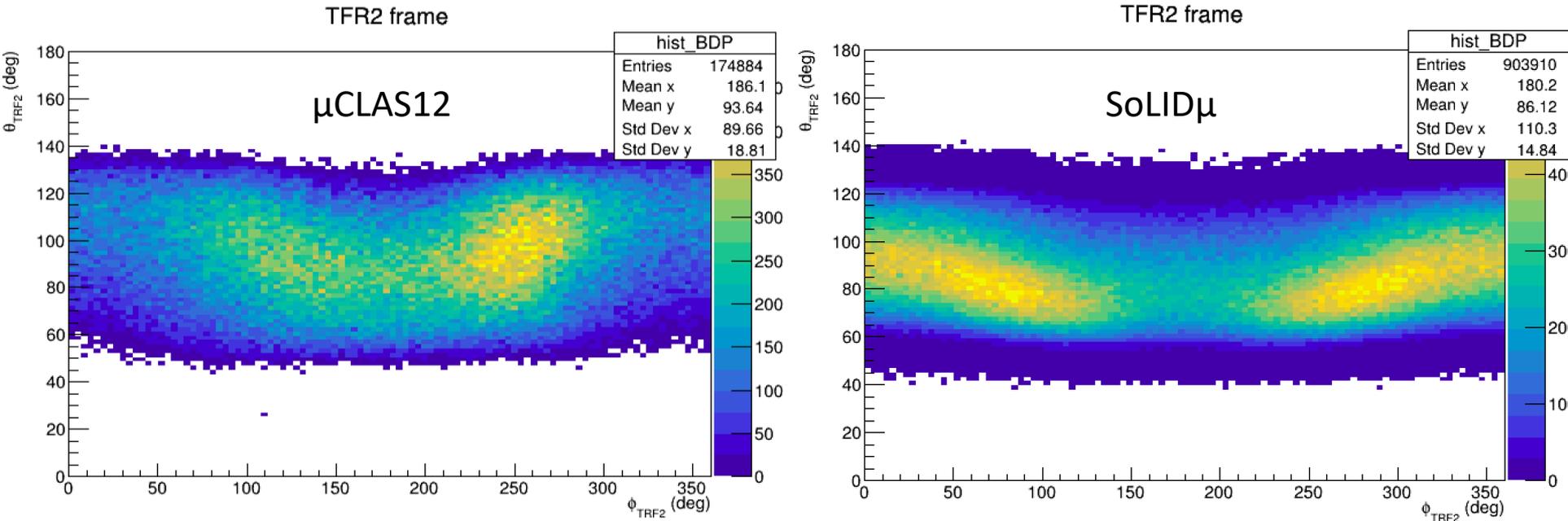


Concept for capacitive charge sharing – K. Gnanvo *et al*, *Nuclear Inst. and Methods in Physics Research, A 1047 (2023) 167782*

SoLID μ vs μ CLAS12

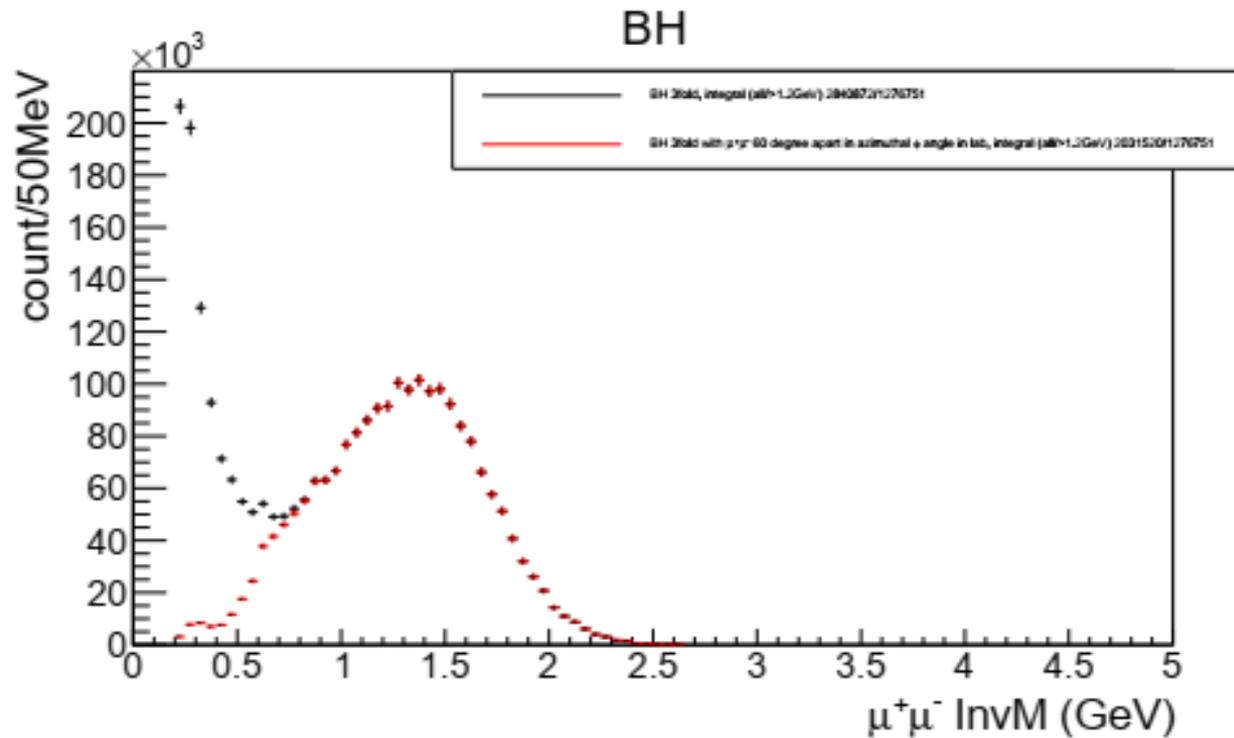


SoLID μ vs μ CLAS12



- Angles in the muon center-of-mass frame
- Larger coverage with SoLID μ

BH and trigger



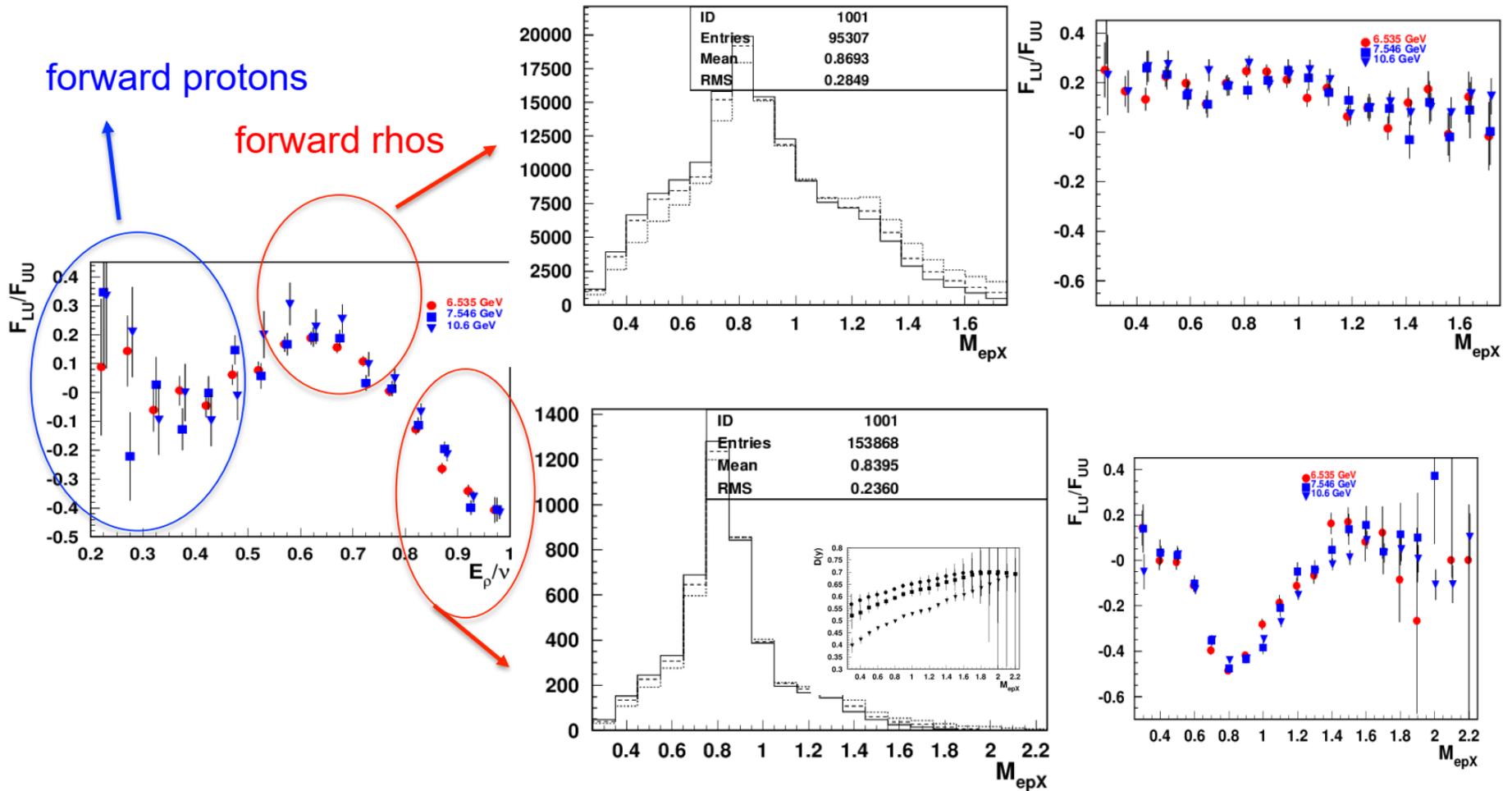
Systematic effects

- Systematics of the measurements will be controlled via **simulations** and the measurement of **reference processes**. The **solenoidal field** and the **symmetrical configuration** of SoLID μ offer further cross-checks
- **Muon solid angle** : extensive simulations based on the **SoLID μ GEANT4 model** ($\delta\Delta\theta_\mu/\Delta\theta_\mu \sim 3\%$)
- **Electron detection efficiency** : measurement of **DIS** and **elastic electron scattering** ($\delta\epsilon_e/\epsilon_e \sim 7\%$)
- **Muon detection efficiency** : measurement of **Bethe-Heitler** and comparison of the **e^\pm** and **μ^\pm decay** of specific meson ($\phi, J/\Psi$) ($\delta\epsilon_\mu/\epsilon_\mu \sim 15\%$)

Background asymmetry

- signal channel asymmetry $A_s=0.1$ and rate R_s
- background channel asymmetry $A_b=0.5$ and rate R_b
- Background/signal rate $R_b/R_s=0.05$ with error $ER=0.01$
- Rel_Error of $A_s = (A_s - A_b) / (1 - R_b/R_s)^2 * ER / A_s$
 $= (0.1 - 0.5) / (1 - 0.05)^2 * 0.01 / 0.1 = -0.045$
- With those conservative assumptions, background only give about 5% error on signal asymmetry

Exclusive $\pi^+\pi^-$: missing mass dependence



Rhos dominate both exclusive dihadron samples, contributing differently depending on z

Cost

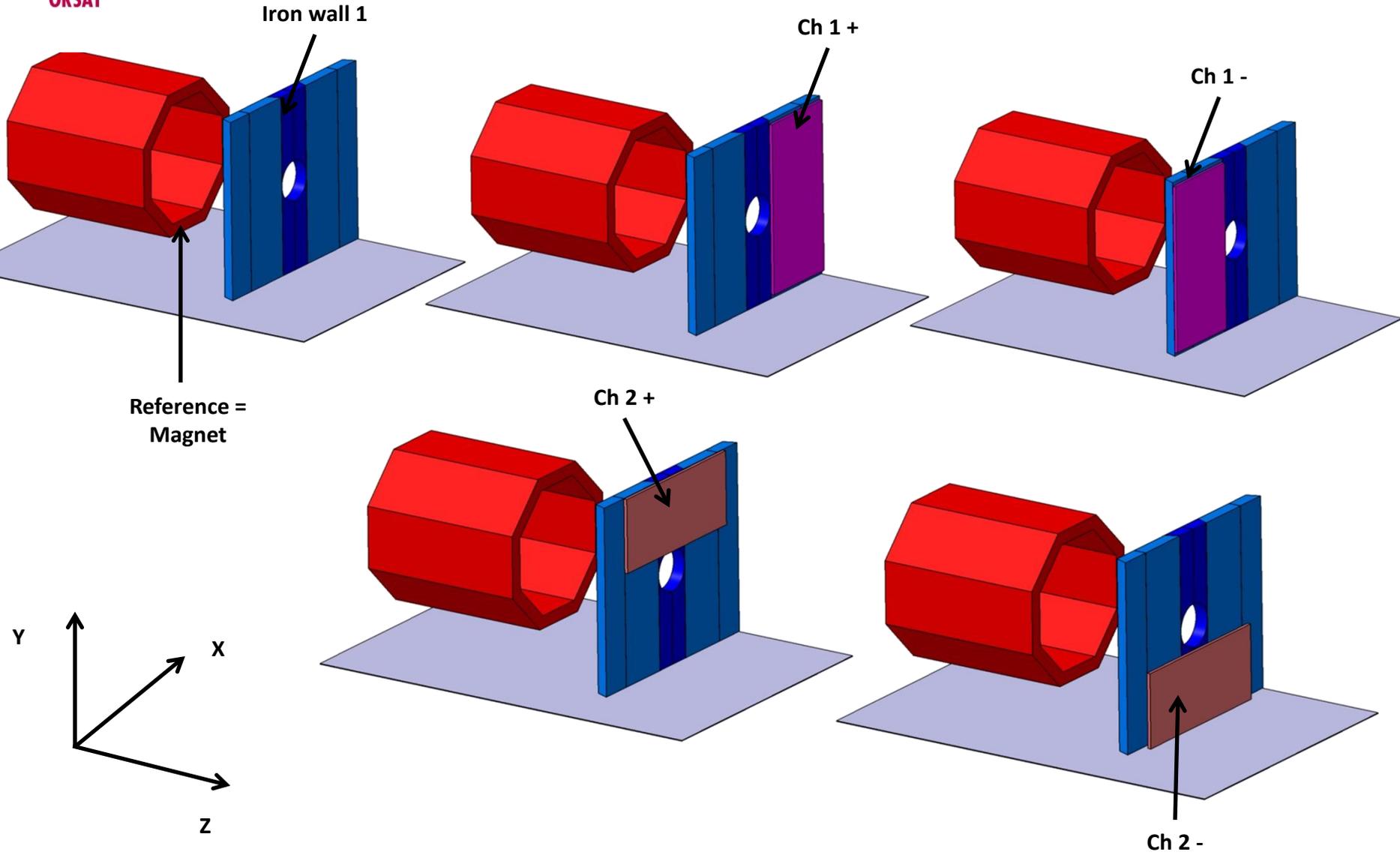
System	Item	Cost (K\$)
Tracker planes	uRWell	900
	VMM readout	300
	HV	10
	Mechanical	100
Scintillator planes	Scint. materials	640
	light guide	180
	PMT+base	180
	FADC	500
	HV	150
	Mechanical	100
Iron planes	Mechanical	200
Total		3,260

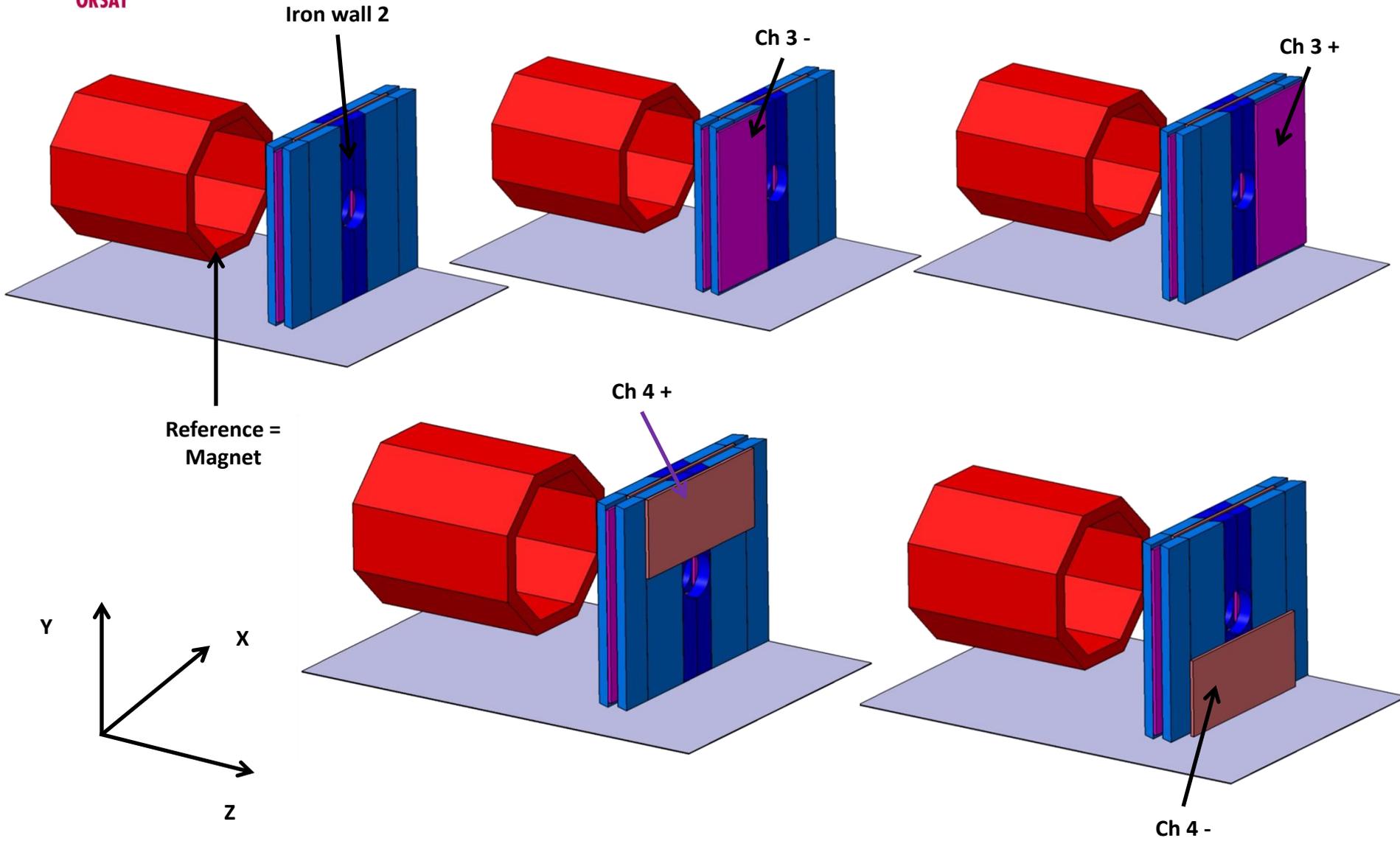
Table 1: Cost estimation of the forward angle muon detector and related hardware.

Binning

Bin	ξ' range	ξ range	t range (GeV ²)
1	$-0.255 < \xi' < 0$	$0.152 < \xi < 0.176$	$-5.541 < t < -0.287$
2			$-0.287 < t < -0.150$
3			$-0.150 < t < -0.020$
4		$0.176 < \xi < 0.739$	$-5.541 < t < -0.287$
5			$-0.287 < t < -0.150$
6			$-0.150 < t < -0.020$
7	$0 < \xi' < 0.512$	$0.071 < \xi < 0.126$	$-5.541 < t < -0.287$
8			$-0.287 < t < -0.150$
9			$-0.150 < t < -0.020$
10		$0.126 < \xi < 0.153$	$-5.541 < t < -0.287$
11			$-0.287 < t < -0.150$
12			$-0.150 < t < -0.020$
13		$0.153 < \xi < 0.189$	$-5.541 < t < -0.287$
14			$-0.287 < t < -0.150$
15			$-0.150 < t < -0.020$
16		$0.189 < \xi < 0.739$	$-5.541 < t < -0.287$
17			$-0.287 < t < -0.150$
18			$-0.150 < t < -0.020$
19	$-0.255 < \xi' < -0.017$	$0.071 < \xi < 0.108$	$-5.541 < t < -0.287$
20			$-0.287 < t < -0.150$
21			$-0.150 < t < -0.020$
22		$0.108 < \xi < 0.122$	$-5.541 < t < -0.287$
23			$-0.287 < t < -0.150$
24			$-0.150 < t < -0.020$
25	$-0.255 < \xi' < -0.040$	$0.122 < \xi < 0.152$	$-5.541 < t < -0.287$
26			$-0.287 < t < -0.150$
27			$-0.150 < t < -0.020$
28	$-0.040 < \xi' < -0.017$	$0.122 < \xi < 0.152$	$-5.541 < t < -0.287$
29			$-0.287 < t < -0.150$
30			$-0.150 < t < -0.020$

Table 2: Bin boundaries of the binning scheme shown in Fig. 24.

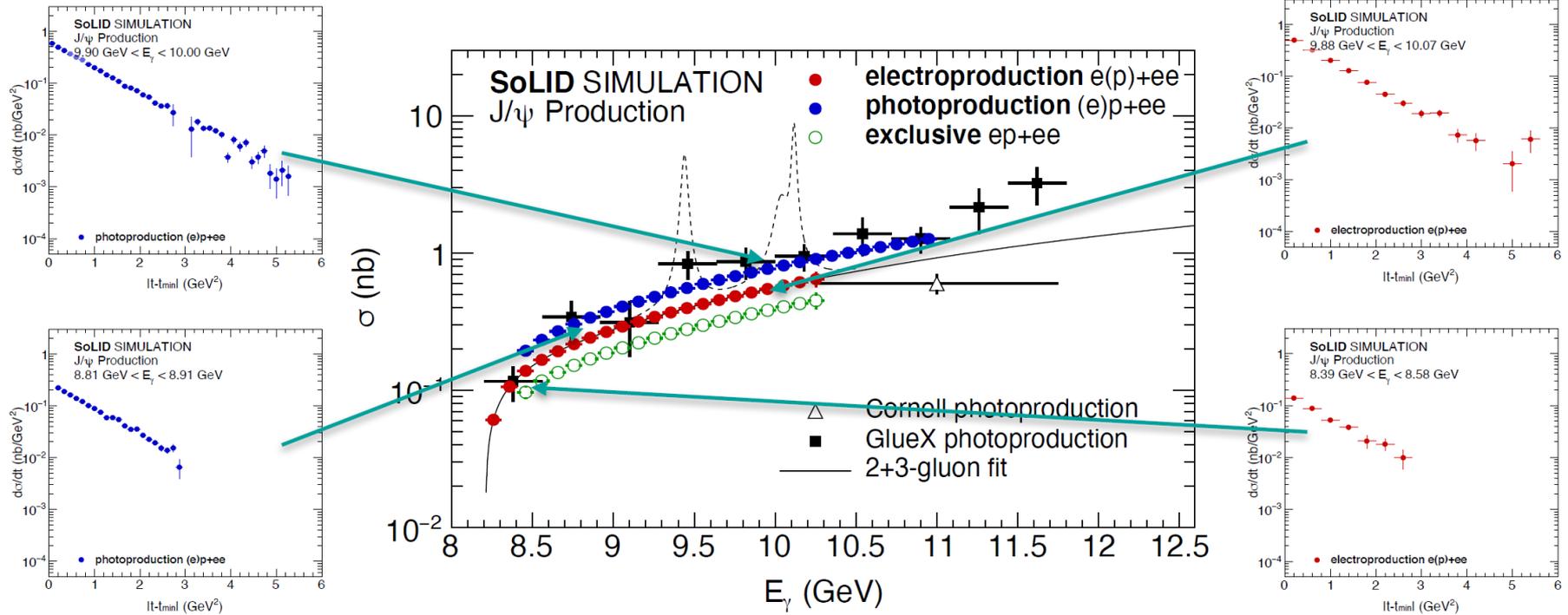




Most precise measurement near threshold

SOLID-J/Ψ PROJECTIONS

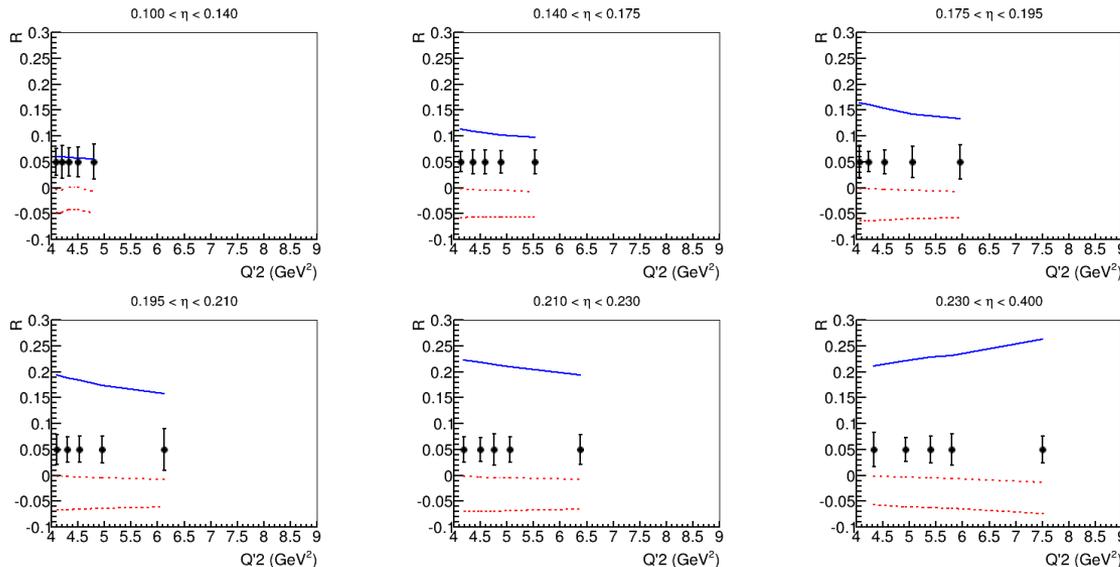
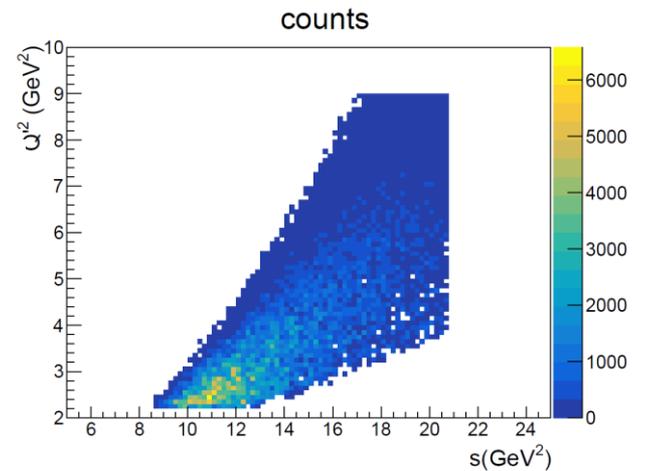
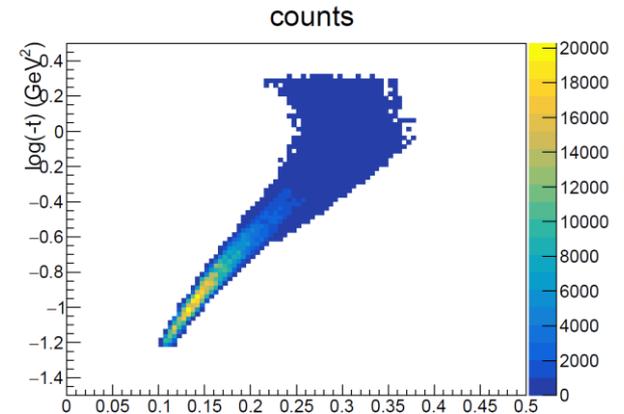
Precision at high t crucial for extrapolations to the forward limit (exponential, dipole, triple, ...)



E12-12-006A: TCS with circular polarized beam and LH2 target

- SoLID TCS will have at least 1 order larger statistics than CLAS12 and usher TCS study into precision era with multi-dimensional binning
 - SoLID has 250 times more integrated luminosity than the CLAS12 TCS published result
 - SoLID acceptance to TCS events is about ¼ of CLAS12. But with full azimuthal coverage, (ideal for the forward backward asymmetry)
 - Crosssection measurement (moment)
- SoLID TCS could lead to study of NLO correction

SoLID TCS coverage



$$R = \frac{2 \int_0^{2\pi} d\phi \cos \phi \frac{dS}{dQ^2 dt d\phi}}{\int_0^{2\pi} d\phi \frac{dS}{dQ^2 dt d\phi}}$$

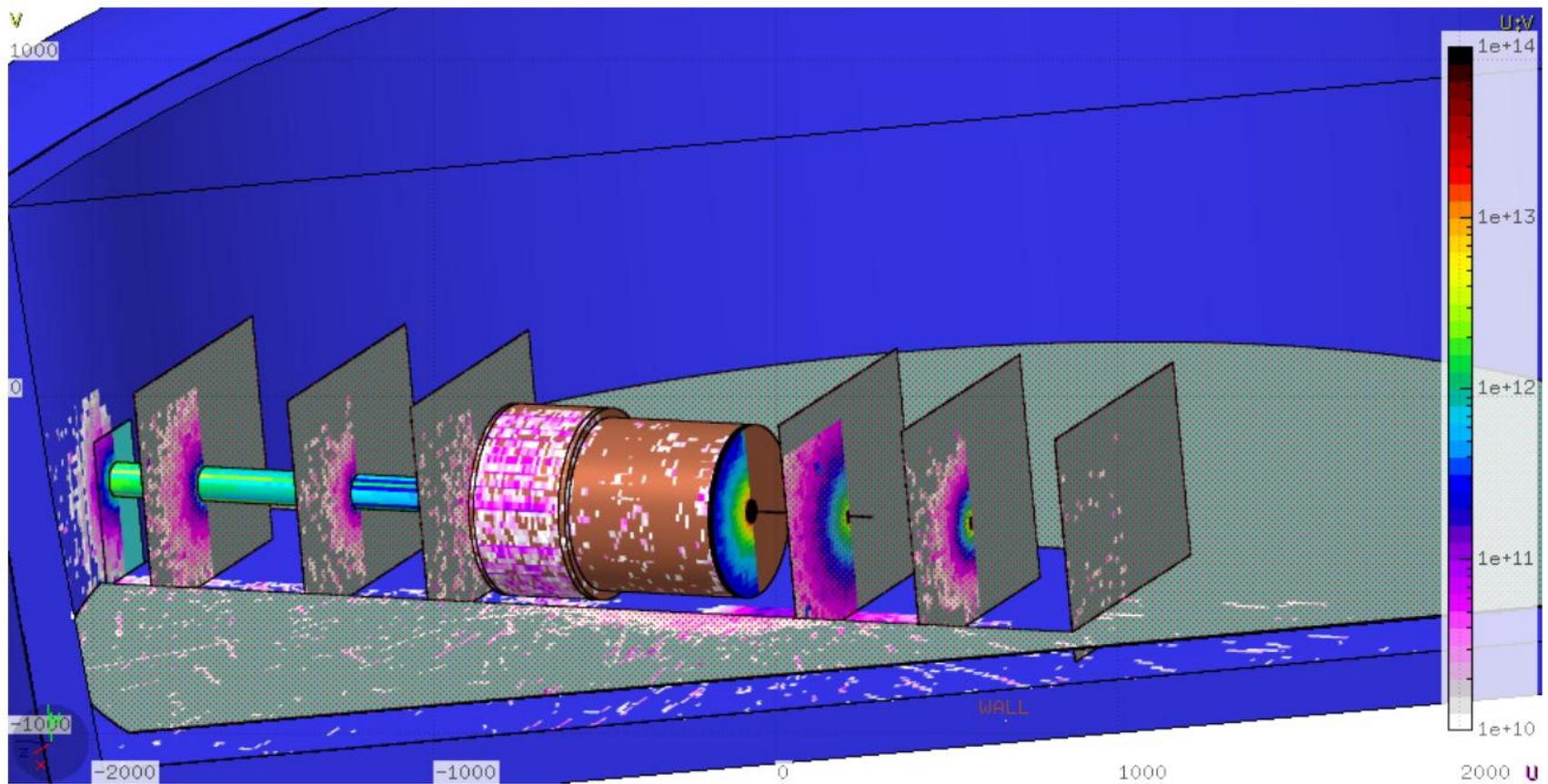


Figure 151: Estimate of radiation damage in the Hall with the SoLID spectrometer and the J/Ψ configuration with a 15cm Liquid Hydrogen target. The leading part of radiation present in the Hall for the SoLID spectrometer is originating from the target area and the closer surface of the magnet. In this plot, we show the 1MeV neutron equivalent flux per cm^2 on the volume surfaces estimated for 60 days of continuous running with a beam current of $3\mu A$ (This is the expected beam-time with the J/Ψ configuration). In order to better show the behavior of the radiation leaking, different planes of observation have been inserted (see Fig. 149a for reference of the position of each plane). The Color scale is different than in the previous cases in order to enhance the details in the desired region.